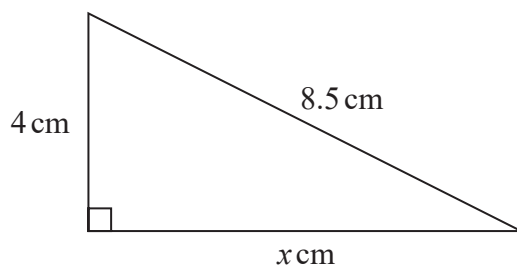


- 1 Here is a right-angled triangle.



Work out the value of x .

$$a^2 + b^2 = c^2$$

$$8.5^2 - 4^2 = x^2$$

$$\begin{array}{r|l} 56.25 & = \\ \sqrt{} & x^2 \\ \hline 7.5 & = \\ & x \end{array}$$

$$x = 7.5$$

(Total for Question 1 is 2 marks)



2 $T = 4m^2 - 11$

(a) Work out the value of T when $m = -3$

$$4(-3)^2 - 11$$

$$T = \frac{25}{(2)}$$

(b) Make p the subject of the formula $d = 3p + 4$

$$\begin{array}{rcl} -4 & & -4 \\ d-4 & = & 3p \\ \div 3 & & \div 3 \\ \frac{d-4}{3} & = & p \end{array}$$

$$p = \frac{d-4}{3} \quad (2)$$

(Total for Question 2 is 4 marks)



- 3 Rick, Selma and Tony are playing a game with counters.

Rick has some counters.

Selma has twice as many counters as Rick.

Tony has 6 counters less than Selma.

In total they have 54 counters.

the number of counters Rick has : the number of counters Tony has = $1 : p$

Work out the value of p .

$$R = x$$

$$S = 2x$$

$$T = 2x - 6$$

$$x + 2x + 2x - 6 = 54$$

$$\begin{array}{rcl} 5x - 6 & = & 54 \\ + 6 & & + 6 \\ \hline 5x & = & 60 \\ \div 5 & & \div 5 \\ \hline x & = & 12 \end{array}$$

$$R = 12$$

$$S = 24$$

$$T = 18$$

$$\begin{array}{l} R : T \\ 12 : 18 \\ \div 12 \quad \downarrow \quad \quad \quad \downarrow \quad \div 12 \\ 1 : 1.5 \end{array}$$

$$p = 1.5$$

(Total for Question 3 is 5 marks)

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DO NOT WRITE IN THIS AREA



- 4 Jo is going to buy 15 rolls of wallpaper.

Here is some information about the cost of rolls of wallpaper from each of two shops.

Chic Decor

3 rolls for £36

Style Papers

Pack of 5 rolls
normal price £70

12% off the normal price

Jo wants to buy the 15 rolls of wallpaper as cheaply as possible.

Should Jo buy the wallpaper from Chic Decor or from Style Papers?

You must show how you get your answer.

Chic Decor

$$\begin{array}{l} 3 \text{ rolls} = £36 \\ \downarrow \times 5 \\ 15 \text{ rolls} = £180 \end{array}$$

Style papers

$$\begin{array}{l} 5 \text{ rolls} = £70 \\ \downarrow \times 3 \\ 15 \text{ rolls} = £210 \end{array}$$

$$12\% \text{ of } 210 = 25.2$$

$$210 - 25.2 = £184.80$$

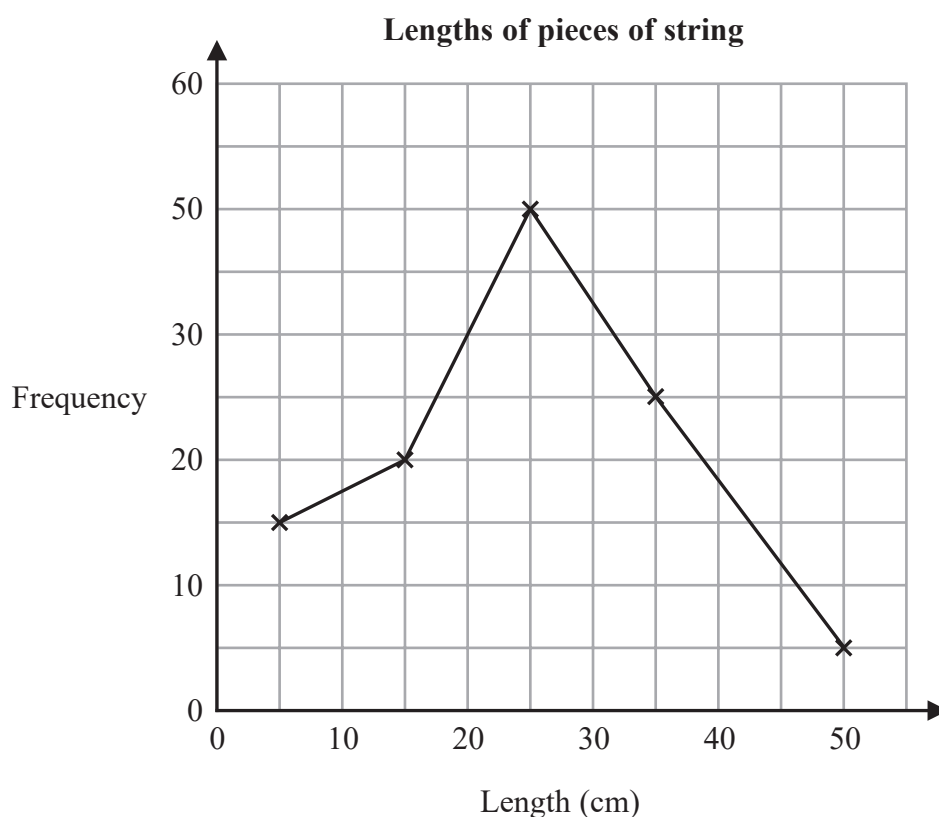
Jo should buy from Chic Decor

(Total for Question 4 is 4 marks)

- 5 The table gives information about the lengths, in cm, of some pieces of string.

Length (t cm)	Frequency
$0 < t \leq 10$	15
$10 < t \leq 20$	20
$20 < t \leq 30$	50
$30 < t \leq 40$	25
$40 < t \leq 50$	5

Amos draws a frequency polygon for the information in the table.



Write down **two** mistakes that Amos has made.

1. The last point has not been plotted at the midpoint
2. 40 is missing from the frequency axis

(Total for Question 5 is 2 marks)



- 6 Jessica runs for 15 minutes at an average speed of 6 miles per hour.
She then runs for 40 minutes at an average speed of 9 miles per hour.

It takes Amy 45 minutes to run the same total distance that Jessica runs.

Work out Amy's average speed.
Give your answer in miles per hour.



Jessica:

Part 1

$$\begin{aligned} S &= 6 \text{ mph} \\ D &= 1.5 \text{ miles} \\ T &= 15 \text{ mins} \end{aligned}$$

Part 2

$$\begin{aligned} S &= 9 \text{ mph} \\ D &= 6 \text{ miles} \\ T &= 40 \text{ mins} \end{aligned}$$

Tip: Remember you can use your time button on a calculator paper!

Distance for part 1: $6 \times 0.15 = 1.5$

Distance for part 2: $9 \times 0.40 = 6$

Amy:

$$\begin{aligned} S &= 10 \text{ mph} \\ D &= 1.5 + 6 = 7.5 \text{ miles} \\ T &= 45 \text{ mins} \end{aligned}$$

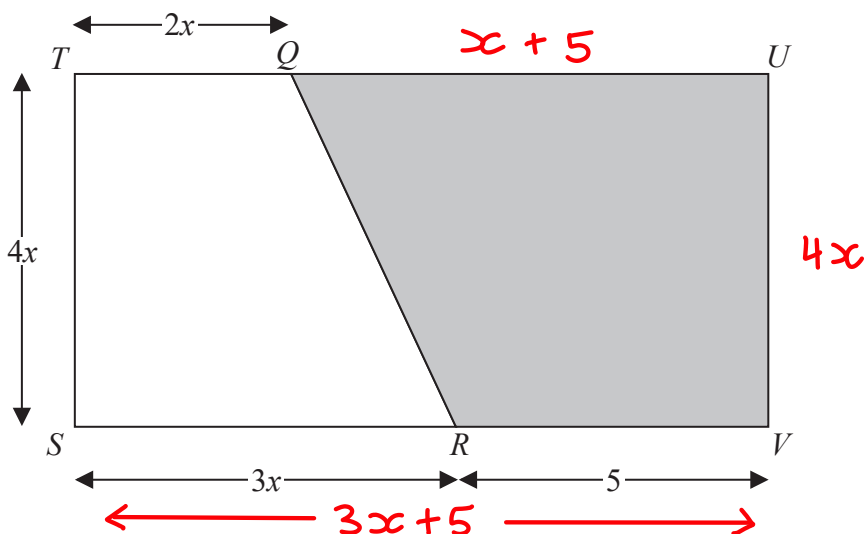
$$S = \frac{7.5}{0.45} = 10$$

.....10..... miles per hour

(Total for Question 6 is 4 marks)

- 7 The diagram shows rectangle $STUV$.
 TQU and SRV are straight lines.
 All measurements are in cm.

$$\text{Area of Trapezium} = \frac{(a+b)h}{2}$$



The area of trapezium $QUVR$ is $A \text{ cm}^2$

Show that $A = 2x^2 + 20x$

Length of QU :

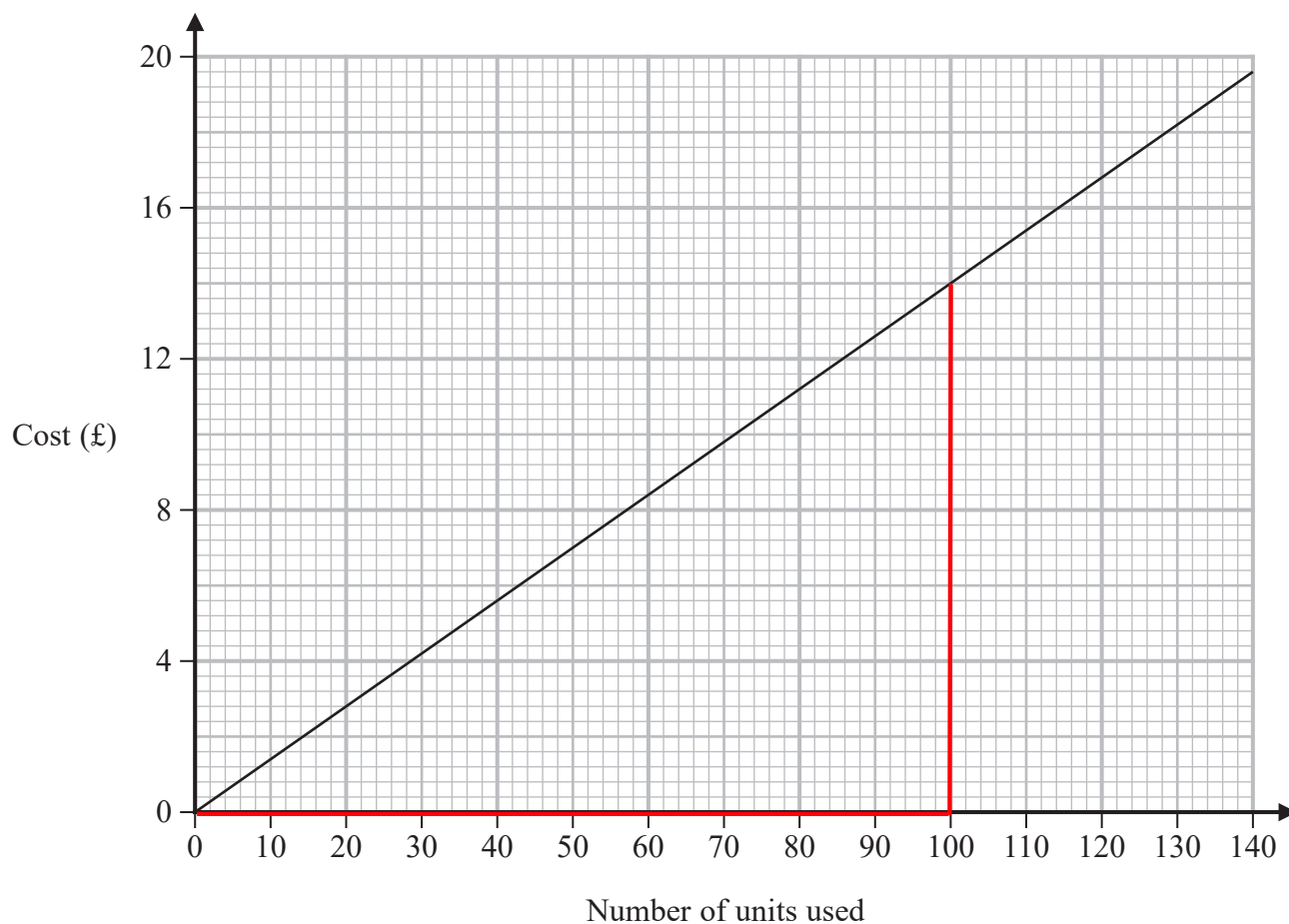
$$3x + 5 - 2x = x + 5$$

$$\begin{aligned} A &= \frac{(x + 5 + 5) \times 4x}{2} = \frac{(x + 10) \times 4x}{2} \\ &= \frac{4x^2 + 40x}{2} \\ &= 2x^2 + 20x \end{aligned}$$

(Total for Question 7 is 3 marks)

- 8 An electricity company charges the same fixed amount for each unit of electricity used.

David uses this graph to work out the total cost of the electricity he has used.



- (a) Work out the gradient of the straight line.

$$\text{Gradient} = \frac{\text{rise}}{\text{run}} = \frac{14}{100} = 0.14$$

0.14
(2)

- (b) What does the gradient of this line represent?

The cost of electricity per unit

(1)

(Total for Question 8 is 3 marks)



- 9 (a) Express $\sqrt{\frac{10^{360}}{10^{150} \times 10^{90}}}$ as a power of 10

$$= \sqrt{\frac{10^{360}}{10^{240}}}$$

$$= \sqrt{10^{120}}$$

$$\frac{10^{60}}{(3)}$$

Liam was asked to express $(12^{50})^2$ as a power of 12

Liam wrote $(12^{50})^2 = 12^{50^2} = 12^{2500}$

Liam's method is wrong.

- (b) Explain why.

$$(12^{50})^2 = 12^{100}$$

(1)

(Total for Question 9 is 4 marks)



10 Jane bought a new car three years ago.

At the end of the first year the value of the car had decreased by 12.5%
The value of the car then decreased by 10% each year for the next two years.

At the end of the three years, the value of the car was £17010

Work out the value of the car when Jane bought it three years ago.

$$\begin{array}{rcl}
 x \times 0.875 \times 0.9^2 & = & 17010 \\
 \div 0.9^2 & & \div 0.9^2 \\
 x \times 0.875 & = & 21000 \\
 \div 0.875 & & \div 0.875 \\
 x & = & 24000
 \end{array}$$

£ 24000

(Total for Question 10 is 3 marks)

11 Rayheem has

16 shirts

5 pairs of jeans

3 jackets

Rayheem chooses an outfit to wear.

An outfit is 1 shirt, 1 pair of jeans and 1 jacket.

Work out how many different outfits Rayheem can choose.

$$16 \times 5 \times 3 = 240$$

240

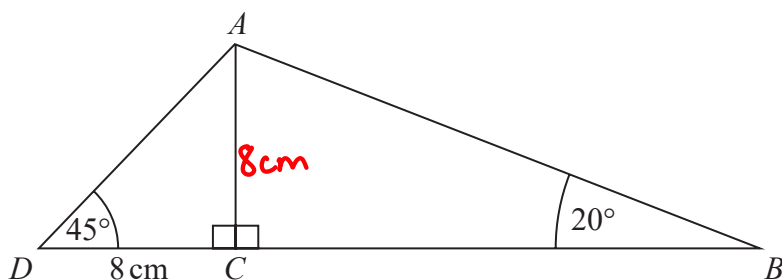
(Total for Question 11 is 2 marks)

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12 ABC and ACD are right-angled triangles.



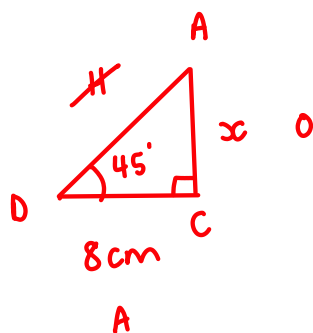
$$DC = 8 \text{ cm}$$

$$\text{Angle } ADC = 45^\circ$$

$$\text{Angle } ABC = 20^\circ$$

Work out the length of AB .

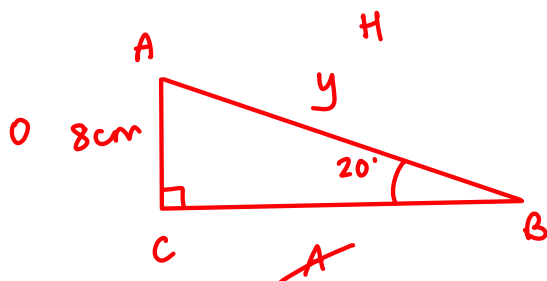
Give your answer correct to 3 significant figures.



S^O H C^A H T^O A

T^O A

$$\tan(45) \times 8 = 8$$



S^O H

$$\frac{8}{\sin(20)} = 23.4$$

23.4

..... cm

(Total for Question 12 is 3 marks)



13 **a** and **b** are vectors such that

$$\mathbf{a} = \begin{pmatrix} 2 \\ -3 \end{pmatrix} \quad \text{and} \quad 3\mathbf{a} - 2\mathbf{b} = \begin{pmatrix} 8 \\ -17 \end{pmatrix}$$

Find **b** as a column vector.

$$3\mathbf{a} = \begin{pmatrix} 6 \\ -9 \end{pmatrix}$$

$$\begin{pmatrix} 6 \\ -9 \end{pmatrix} - \begin{pmatrix} -2 \\ 8 \end{pmatrix} = \begin{pmatrix} 8 \\ -17 \end{pmatrix}$$

$$2\mathbf{b} = \begin{pmatrix} -2 \\ 8 \end{pmatrix}$$

$$\mathbf{b} = \begin{pmatrix} -1 \\ 4 \end{pmatrix}$$

$$\begin{pmatrix} -1 \\ 4 \end{pmatrix}$$

(Total for Question 13 is 3 marks)

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DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



14 (a) Factorise fully $4p^2 - 36$

$$= 4(p-9)$$

$$= 4(p+3)(p-3)$$

$$\underline{4(p+3)(p-3)}$$

(2)

(b) Show that $(m+4)(2m-5)(3m+1)$ can be written in the form $am^3 + bm^2 + cm + d$ where a, b, c and d are integers.

$$(m+4)(2m-5) = 2m^2 - 5m + 8m - 20$$

$$= 2m^2 + 3m - 20$$

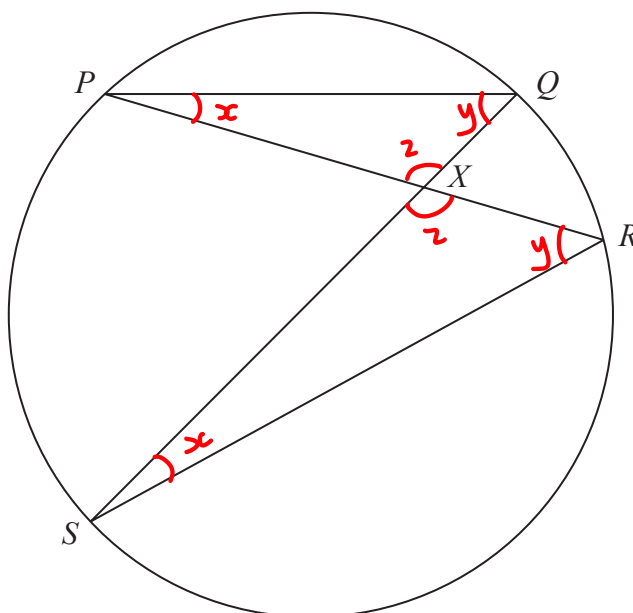
$$(2m^2 + 3m - 20)(3m+1) = 6m^3 + 2m^2 + 9m^2 + 3m - 60m - 20$$

$$= 6m^3 + 11m^2 - 57m - 20$$

(3)

(Total for Question 14 is 5 marks)

15 P, Q, R and S are four points on a circle.



PXR and SXQ are straight lines.

Prove that triangle PQX and triangle SRX are similar.

$$\left. \begin{array}{l} \angle QPX = \angle XSR \\ \angle PQX = \angle XRS \end{array} \right\} \text{Angles in the same segment are equal}$$

$$\angle QXP = \angle RXS \quad \text{Vertically opposite angles are equal}$$

(Total for Question 15 is 3 marks)



$$16 \quad p = \sqrt{\frac{2e}{f}}$$

$$LB = 6.75 \quad UB = 6.85$$

$e = 6.8$ correct to 1 decimal place.

$f = 0.05$ correct to 1 significant figure.

$$LB = 0.045 \quad UB = 0.055$$

Work out the upper bound for the value of p .

Give your answer correct to 3 significant figures.

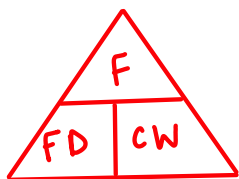
You must show all your working.

$$p_u = \sqrt{\frac{2e_u}{f_l}} = \sqrt{\frac{2(6.85)}{0.045}} = 17.4483..$$

17.4

(Total for Question 16 is 3 marks)

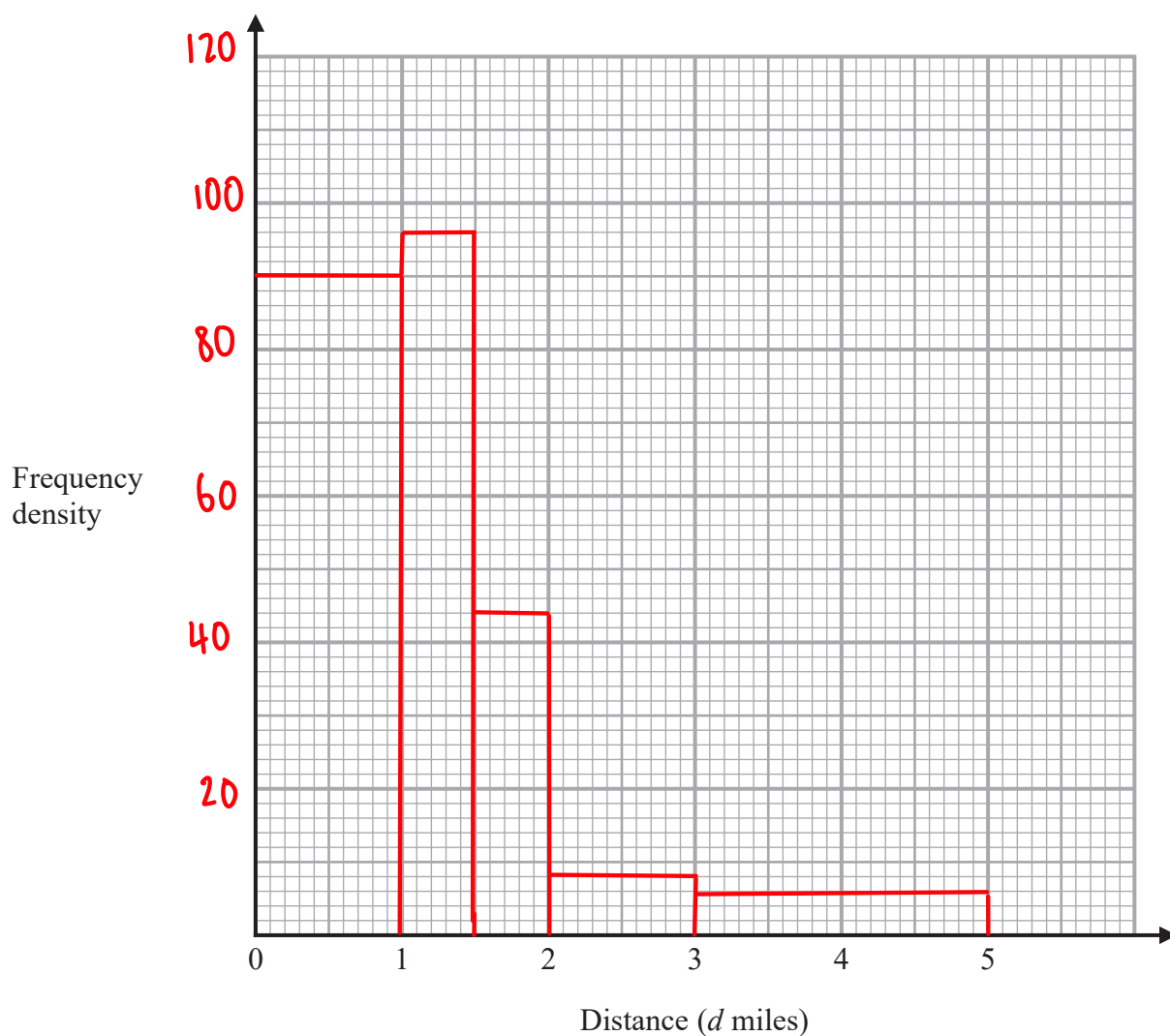
- 17 The table gives information about the distances, in miles, that some Year 10 students live from school.



Distance (d miles)	Frequency
$0 < d \leq 1.0$	90
$1.0 < d \leq 1.5$	48
$1.5 < d \leq 2.0$	22
$2.0 < d \leq 3.0$	8
$3.0 < d \leq 5.0$	12

FD
90
96
44
8
6

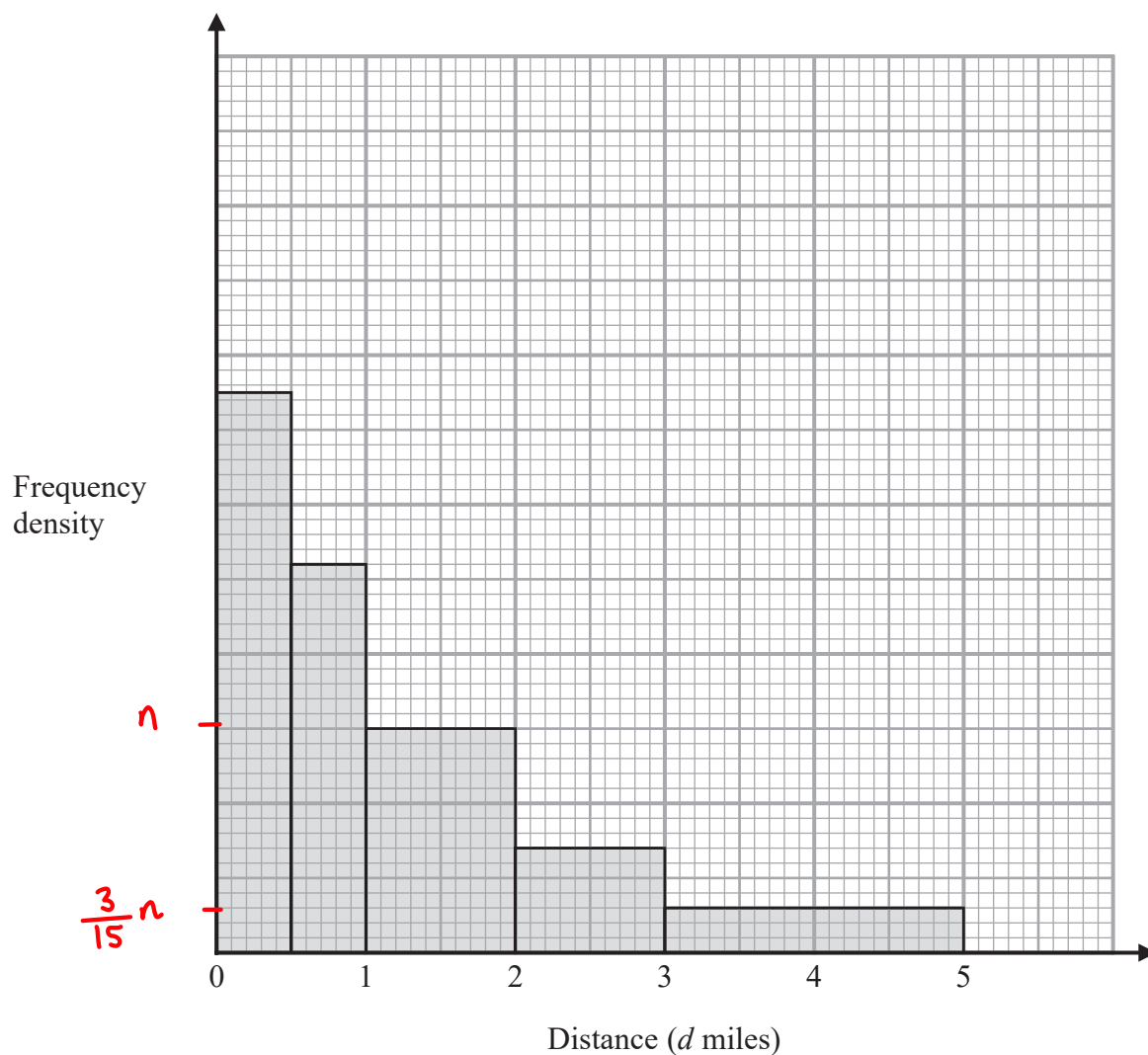
- (a) On the grid, draw a histogram for this information.



(3)



The histogram below shows information about the distances, in miles, that some Year 11 students live from school.



The number of Year 11 students who live between 1 and 2 miles from school is n .

- (b) Find an expression, in terms of n , for the number of Year 11 students who live between 3 and 5 miles from school.

$$FD = \frac{F}{CW} = \frac{n}{1} = n$$

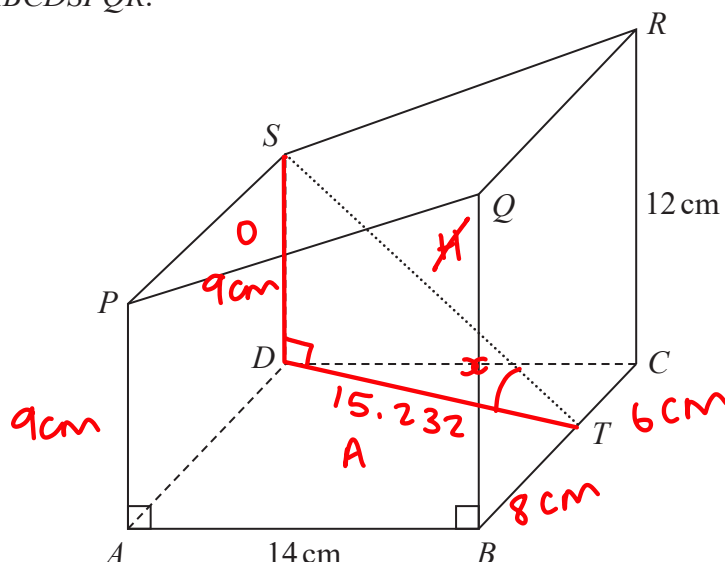
$$F = FD \times CW = \frac{3}{15}n \times 2 = \frac{2}{5}n$$

$$\frac{2}{5}n$$

(2)

(Total for Question 17 is 5 marks)

18 Here is a prism $ABCDSPQR$.



The base $ABCD$ of the prism is a square of side 14 cm

T is the point on BC such that $BT : TC = 4 : 3$ (7 parts)

The cross section of the prism is in the shape of a trapezium of area 147 cm^2

$CR = 12 \text{ cm}$

Find the size of the angle between the line ST and the base $ABCD$.

Give your answer correct to 1 decimal place.

$$14 \div 7 = 2 \text{ (1 part)} \quad \begin{array}{l} 4 \times 2 = 8 \text{ cm} \\ 3 \times 2 = 6 \text{ cm} \end{array}$$

$$\text{Area of Trapezium} = \frac{(a+b)h}{2}$$

$$\begin{array}{rcl} \frac{(a+12) \times 14}{2} & = & 147 \\ (a+12) \times 14 & = & 294 \\ a+12 & = & 21 \\ a & = & 9 \end{array}$$

$$\tan^{-1} \left(\frac{9}{15.232} \right) =$$

$$DT = 6^2 + 14^2 = 232$$

$$\sqrt{232} = 15.232$$

$$30.6^\circ$$

(Total for Question 18 is 5 marks)



- 19 Show that $\frac{3x}{x+2} - \frac{2x+1}{x-2} - 1$ can be written in the form $\frac{ax+b}{x^2-4}$ where a and b are integers.

$$= \frac{x^2-4}{(x+2)(x-2)}$$

$$\frac{3x(x-2)}{x^2-4} - \frac{(2x+1)(x+2)}{x^2-4} - \frac{x^2-4}{x^2-4}$$

$$= \frac{3x^2-6x}{x^2-4} - \frac{2x^2+5x+2}{x^2-4} - \frac{x^2-4}{x^2-4}$$

$$= \frac{-11x+2}{x^2-4}$$

(Total for Question 19 is 4 marks)

20 The profit made by a shop increases each year.

The profit made by the shop in year n is $\text{£}P_n$

Given that the profit made by the shop in the next year is $\text{£}P_{n+1}$ then

$$P_{n+1} = aP_n + 800 \text{ where } a \text{ is a constant.}$$

$$a = 1.2$$

The table shows the profit made by the shop in 2018 and in 2019

Year	2018 P_0	2019 P_1
Profit	£24 000	£29 600

Work out the profit predicted to be made by the shop in 2021

$$P_0 = 24000$$

$$P_1 = a(24000) + 800$$

$$\begin{array}{r|l} 24000a + 800 & = 29600 \\ - 800 & - 800 \\ \hline 24000a & = 28800 \\ \div 24000 & \div 24000 \\ \hline a & = 1.2 \end{array}$$

$$P_2 = 1.2(29600) + 800 = 36320$$

$$P_3 = 1.2(36320) + 800 = 44384$$

£ 44384

(Total for Question 20 is 4 marks)



21 Ray has nine cards numbered 1 to 9



Ray takes at random three of these cards.

He works out the sum of the numbers on the three cards and records the result.

Work out the probability that the result is an even number.

ways to get an even number :

$$E + E + E = \frac{4}{9} \times \frac{3}{8} \times \frac{2}{7} = \frac{1}{21}$$

$$O + O + E = \frac{5}{9} \times \frac{4}{8} \times \frac{4}{7} = \frac{10}{63}$$

$$O + E + O = \frac{5}{9} \times \frac{4}{8} \times \frac{4}{7} = \frac{10}{63}$$

$$O + O + E = \frac{5}{9} \times \frac{4}{8} \times \frac{4}{7} = \frac{10}{63}$$

$$\frac{1}{21} + \frac{10}{63} + \frac{10}{63} + \frac{10}{63} = \frac{11}{21}$$

$$\frac{11}{21}$$

(Total for Question 21 is 4 marks)

22 L is the straight line with equation $y = 2x - 5$

C is a graph with equation $y^2 = 6x^2 - 25x - 8$

Using algebra, find the coordinates of the points of intersection of L and C.
You must show all your working.

$$y = 2x - 5$$

$$y^2 = (2x - 5)(2x - 5) = 4x^2 - 20x + 25$$

$$y^2 = 6x^2 - 25x - 8$$

Tip: Because we have y^2 as the subject of both equations, we can make them equal to each other and solve to find the values of x

$$6x^2 - 25x - 8 = 4x^2 - 20x + 25$$

$$2x^2 - 5x - 33 = 0$$

$$2x^2 - 11x + 6x - 33 = 0$$

$$x(2x - 11) + 3(2x - 11) = 0$$

$$(x + 3)(2x - 11) = 0$$

$$x = -3$$

$$x = \frac{11}{2} \text{ or } 5.5$$

$$y = 2x - 5$$

when $x = -3$

$$y = 2(-3) - 5 = -11$$

$$(-3, -11)$$

when $x = 5.5$

$$y = 2(5.5) - 5 = 6$$

$$(5.5, 6)$$

(Total for Question 22 is 5 marks)

TOTAL FOR PAPER IS 80 MARKS