

1 Solve $5x - 6 = 3(x - 1)$

$$\begin{array}{rcl} 5x - 6 & = & 3x - 3 \\ -3x & & -3x \\ \hline 2x - 6 & = & -3 \\ +6 & & +6 \\ \hline 2x & = & 3 \\ \div 2 & & \div 2 \\ \hline x & = & 3/2 \end{array}$$

$$x = \frac{3}{2} \text{ or } 1.5$$

(Total for Question 1 is 3 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- 2 Emily buys a pack of 12 bottles of water.
The pack costs £5.64

Emily sells all 12 bottles for 50p each.

Work out Emily's percentage profit.
Give your answer correct to 1 decimal place.

$$\frac{\text{change}}{\text{original}} \times 100$$

$$12 \times 0.5 = £6$$

$$\frac{6 - 5.64}{5.64} \times 100 = 6.3829...$$

$$6.4\%$$

(Total for Question 2 is 3 marks)

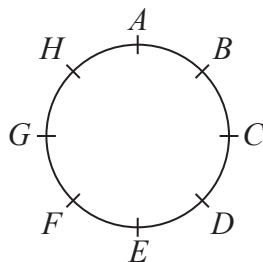
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



- 3 Hasmeet walks once round a circle with diameter 80 metres.



There are 8 points equally spaced on the circumference of the circle.

- (a) Find the distance Hasmeet walks between one point and the next point.

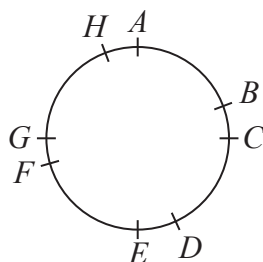
$$\pi \times 80 = 80\pi$$

$$\div 8 = 10\pi$$

$$\underline{31.4} \text{ m}$$

(2)

Four of the points are moved, as shown in the diagram below.



Hasmeet walks once round the circle again.

- (b) Has the mean distance that Hasmeet walks between one point and the next point changed?
You must give a reason for your answer.

NO, the distance and number of points
is the same

(1)

(Total for Question 3 is 3 marks)

- 4 There are only blue cubes, yellow cubes and green cubes in a bag.

There are

twice as many blue cubes as yellow cubes
and four times as many green cubes as blue cubes.

Hannah takes at random a cube from the bag.

Work out the probability that Hannah takes a yellow cube.

$$\begin{array}{ll} B : 4 & G : 8 \\ 2 : 1 & 4 : 1 \\ 2 : 1 & 8 : 2 \end{array} \quad \begin{array}{l} \text{) } \\ \text{ } \end{array} \times 2$$

$$\begin{array}{l} B : 4 : 8 \\ 2 : 1 : 2 \end{array}$$

$$\frac{1}{11}$$

(Total for Question 4 is 3 marks)

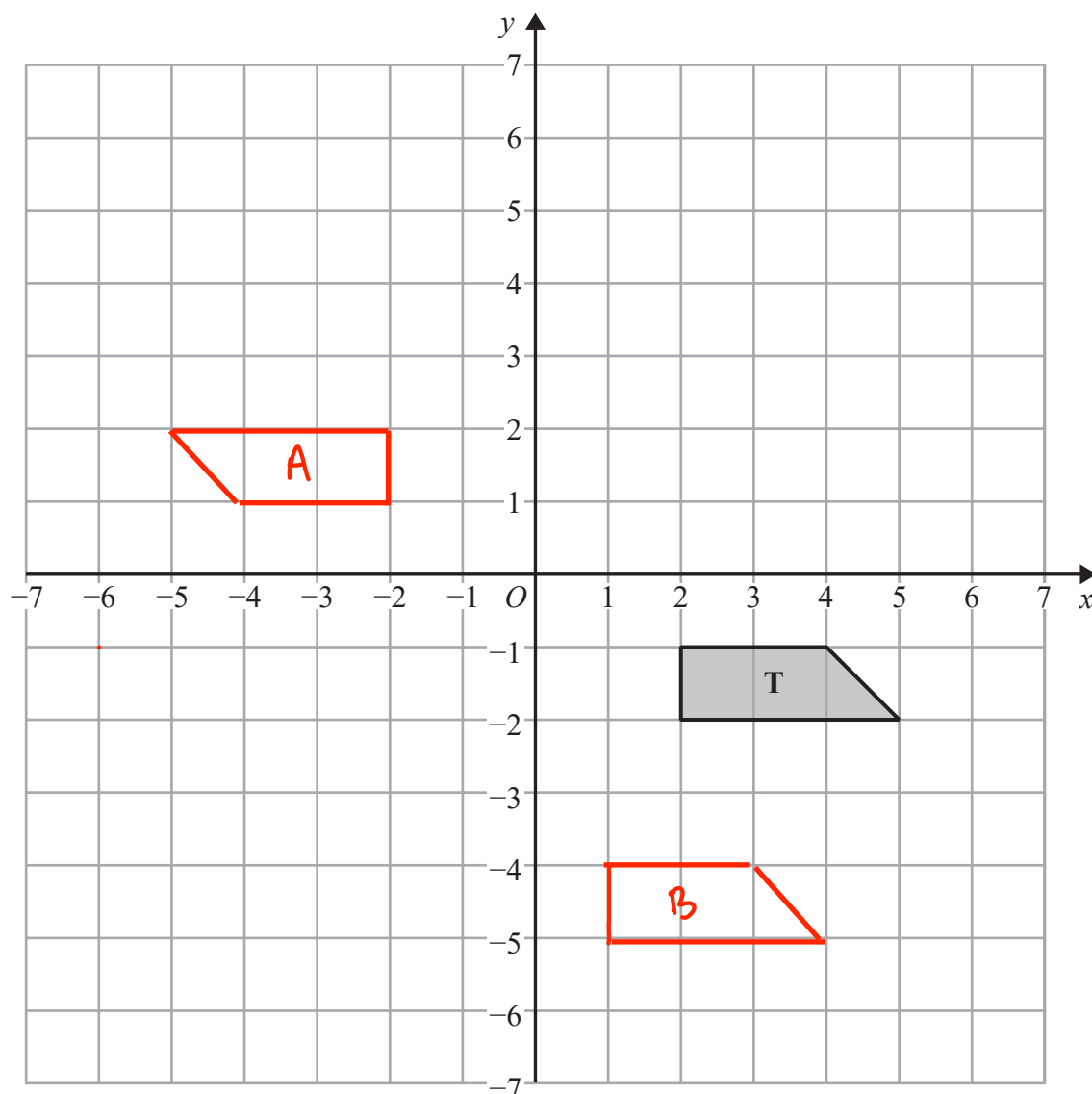
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



5



- (a) Rotate trapezium **T** 180° about the origin.
Label the new trapezium **A**.

(1)

- (b) Translate trapezium **T** by the vector $\begin{pmatrix} -1 \\ -3 \end{pmatrix}$
Label the new trapezium **B**.

(1)

(Total for Question 5 is 2 marks)

6 $p^3 \times p^x = p^9$

(a) Find the value of x .

$$x = \overset{6}{\dots\dots\dots} \quad (1)$$

$$(7^2)^y = 7^{10}$$

(b) Find the value of y .

$$y = \overset{5}{\dots\dots\dots} \quad (1)$$

$100^a \times 1000^b$ can be written in the form 10^w

(c) Show that $w = 2a + 3b$

$$\begin{aligned} & (10^2)^a \times (10^3)^b \\ &= 10^{2a} \times 10^{3b} \\ &= 10^{2a+3b} \end{aligned}$$

$$\therefore w = 2a + 3b$$

(2)

(Total for Question 6 is 4 marks)

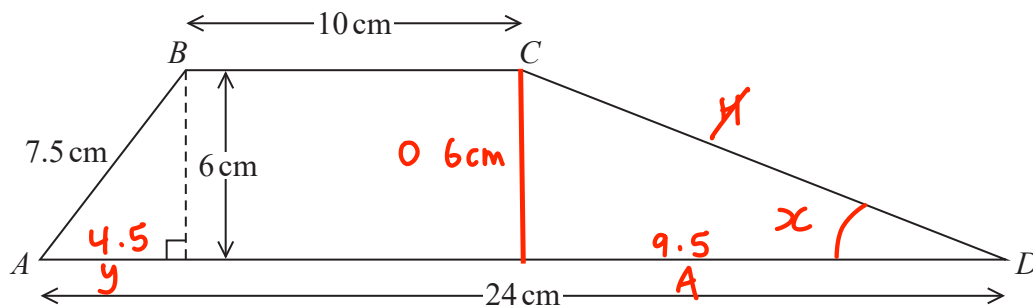
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



7 $ABCD$ is a trapezium.



Work out the size of angle CDA .

Give your answer correct to 1 decimal place.

$$y^2 = 7.5^2 - 6^2 = 20.25$$

$$\sqrt{20.25} = 4.5$$

$$24 - 10 - 4.5 = 9.5$$

$$\tan^{-1}\left(\frac{6}{9.5}\right) = 32.27..$$

$$S^{\circ} H \quad C^A H \quad \cancel{A^{\circ}}$$

32.3

(Total for Question 7 is 5 marks)

8 Use your calculator to work out $\sqrt{\frac{\sin 25^\circ + \sin 40^\circ}{\cos 25^\circ - \cos 40^\circ}}$

(a) Write down all the figures on your calculator display.

2.75603957

(2)

(b) Write your answer to part (a) correct to 2 decimal places.

2.76

(1)

(Total for Question 8 is 3 marks)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

- 9 Yesterday it took 5 cleaners $4\frac{1}{2}$ hours to clean all the rooms in a hotel.

There are only 3 cleaners to clean all the rooms in the hotel today.

Each cleaner is paid £8.20 for each hour or part of an hour they work.

How much will each cleaner be paid today?

$$\begin{array}{lcl} \div 5 & \downarrow & 5 \text{ cleaners} = 4.5 \text{ hours} \\ & & \downarrow \times 5 \\ & & 1 \text{ cleaner} = 22.5 \text{ hours} \\ \times 3 & \downarrow & 3 \text{ cleaners} = 7.5 \text{ hours} \\ & & \downarrow \div 3 \end{array}$$

$$8.20 \times 8 = 65.60$$

£ 65.60

(Total for Question 9 is 3 marks)

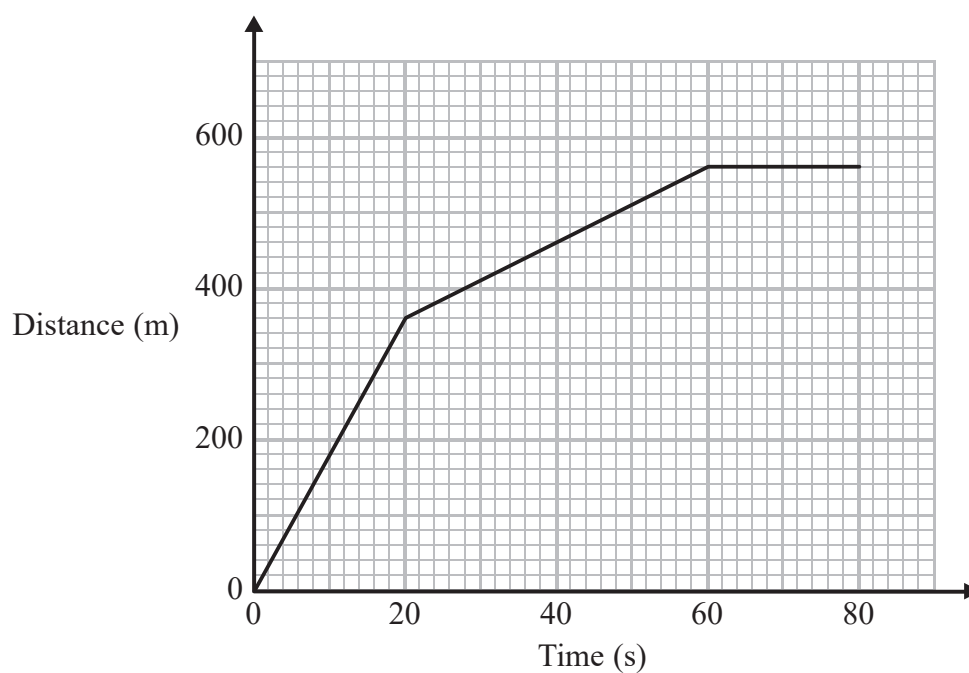
DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



10 Here is part of a distance-time graph for a car's journey.



- (a) Between which two times does the car travel at its greatest speed?
Give a reason for your answer.

Between 0-20 seconds, the gradient is the steepest

(2)

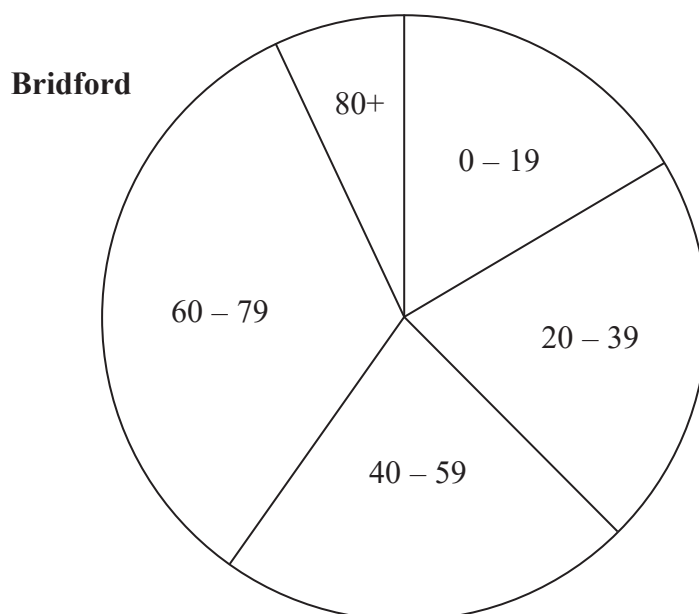
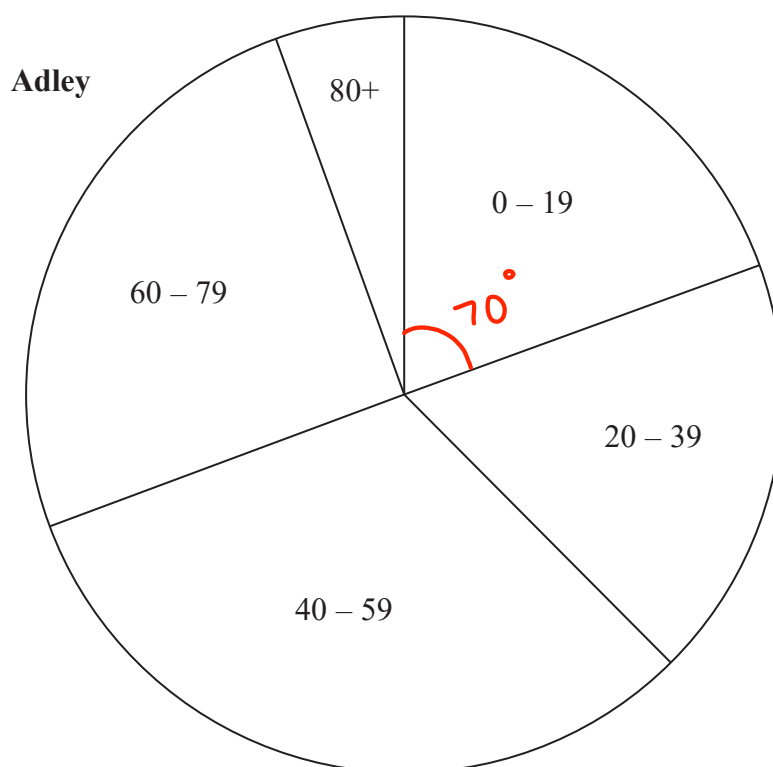
- (b) Work out this greatest speed.

$$S = \frac{D}{T} = \frac{360}{20} = 18$$

18 m/s
(1)

(Total for Question 10 is 3 marks)

- 11 The pie charts give information about the ages, in years, of people living in two towns, Adley and Bridford.



The ratio of the number of people living in Adley to the number of people living in Bridford is given by the **ratio of the areas** of the pie charts.

What proportion of the total number of people living in these two towns live in Adley **and** are aged 0 – 19?

Give your answer correct to 3 significant figures.

$$\begin{aligned}\text{Adley area} &= \pi \times 5^2 = 25\pi \\ \text{Bridford area} &= \pi \times 4^2 = 16\pi \\ \hline &41\pi\end{aligned}$$

$$\begin{aligned}A : B \\ 25 : 16\end{aligned}$$

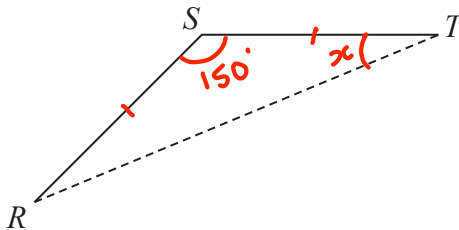
$$\text{Adley 0-19 area} = \frac{70}{360} \times 25\pi = 15.27163095$$

$$\frac{15.2716...}{41\pi} = 0.1185..$$

$$0.119$$

(Total for Question 11 is 3 marks)

12



RS and ST are 2 sides of a regular 12-sided polygon.
 RT is a diagonal of the polygon.

Work out the size of angle STR .
You must show your working.

$$(12 - 2) \times 180 = 1800$$

$$1800 \div 12 = 150$$

$$180 - 150 = 30$$

$$30 \div 2 = 15$$

15

(Total for Question 12 is 3 marks)

- 13 At the beginning of 2009, Mr Veale bought a company.
The value of the company was £50 000

Each year the value of the company increased by 2%.

- (a) Calculate the value of the company at the beginning of 2017
Give your answer correct to the nearest £100

$$50,000 \times 1.02^8 = 58582.969..$$

£ 58600
(2)

At the beginning of 2009 the value of a different company was £250 000
In 6 years the value of this company increased to £325 000

This is equivalent to an increase of $x\%$ each year.

- (b) Find the value of x .
Give your answer correct to 2 significant figures.

$$\begin{array}{rcl} 250000 \times y^6 & = & 325000 \\ \div 250000 & & \div 250000 \\ y^6 & = & 1.3 \\ \sqrt[6]{} & & \sqrt[6]{} \\ y & = & 1.04469... \end{array}$$

4.5% increase

4.5
(3)

(Total for Question 13 is 5 marks)



14 On the grid, shade the region that satisfies all these inequalities.

$$y > 1$$

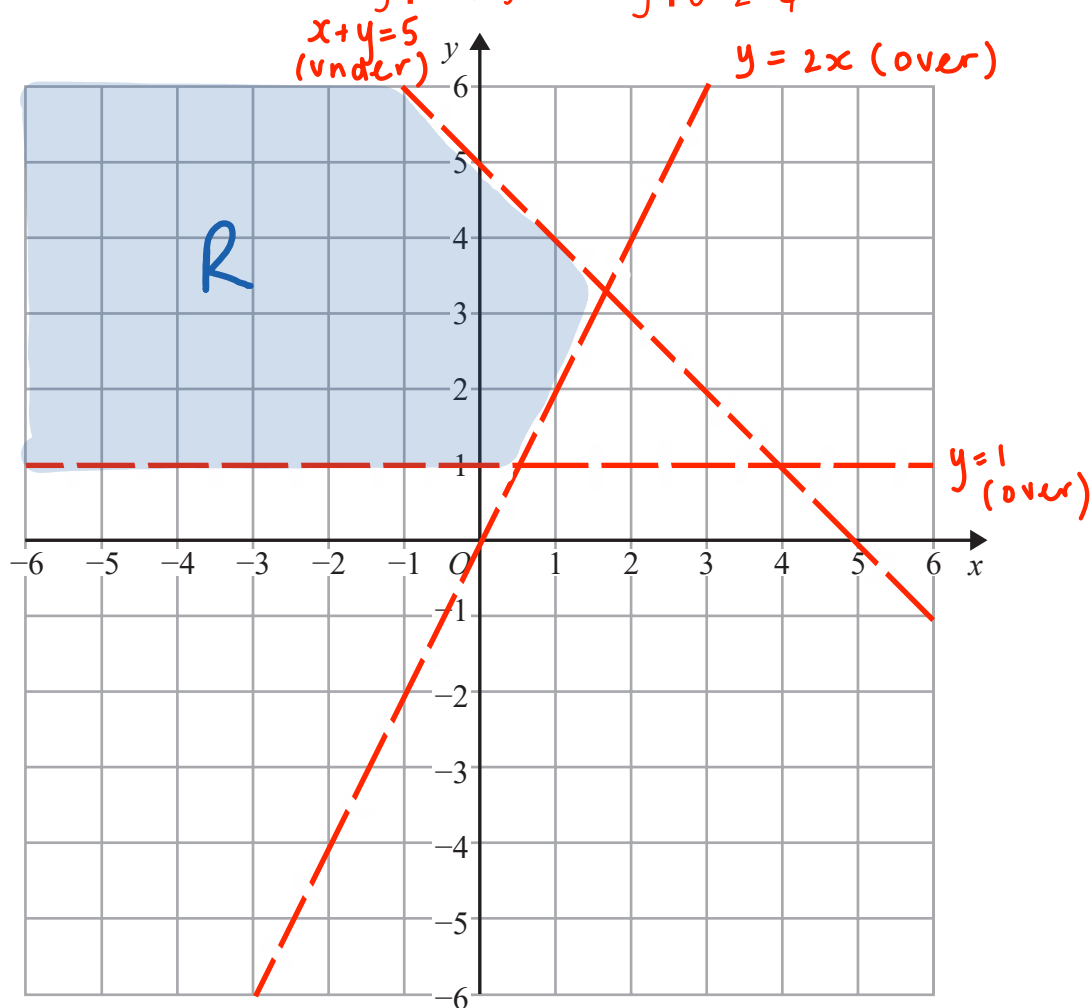
$$x + y < 5$$

$$y > 2x$$

Label the region **R**.

x	0	1	2
y	5	4	3

x	0	1	2
y	0	2	4



(Total for Question 14 is 3 marks)

- 15 Tracey is going to choose a main course and a dessert in a cafe.
She can choose from 8 main courses and 7 desserts.

Tracey says that to work out the number of different ways of choosing a main course and a dessert you add 8 and 7

- (a) Is Tracey correct?

You must give a reason for your answer.

No, you need to multiply 8 and 7

(1)

12 teams play in a competition.

Each team plays each other team exactly once.

- (b) Work out the total number of games played.

$$12 \times 11 = 132$$

$$132 \div 2 = 66$$

(2)

(Total for Question 15 is 3 marks)

16 Solve $(x - 2)^2 = 3$

Give your solutions correct to 3 significant figures.

$$\begin{aligned}
 (x - 2)(x - 2) &= 3 \\
 x^2 - 2x - 2x + 4 &= 3 \\
 x^2 - 4x + 4 &= 3 \\
 &\quad -3 \quad \quad -3 \\
 x^2 - 4x + 1 &= 0
 \end{aligned}$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = 1 \quad b = -4 \quad c = 1$$

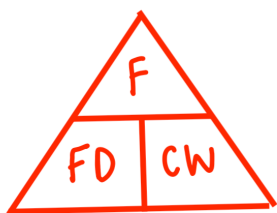
$$\frac{-(-4) \pm \sqrt{(-4)^2 - 4(1)(1)}}{2(1)}$$

$$x = 3.73, x = 0.268$$

(Total for Question 16 is 2 marks)



17 The table gives information about the heights of 150 students.



Height (h cm)	Frequency
$140 < h \leq 150$	15
$150 < h \leq 155$	30
$155 < h \leq 160$	51
$160 < h \leq 165$	36
$165 < h \leq 180$	18

FD

$$15 \div 10 = 1.5$$

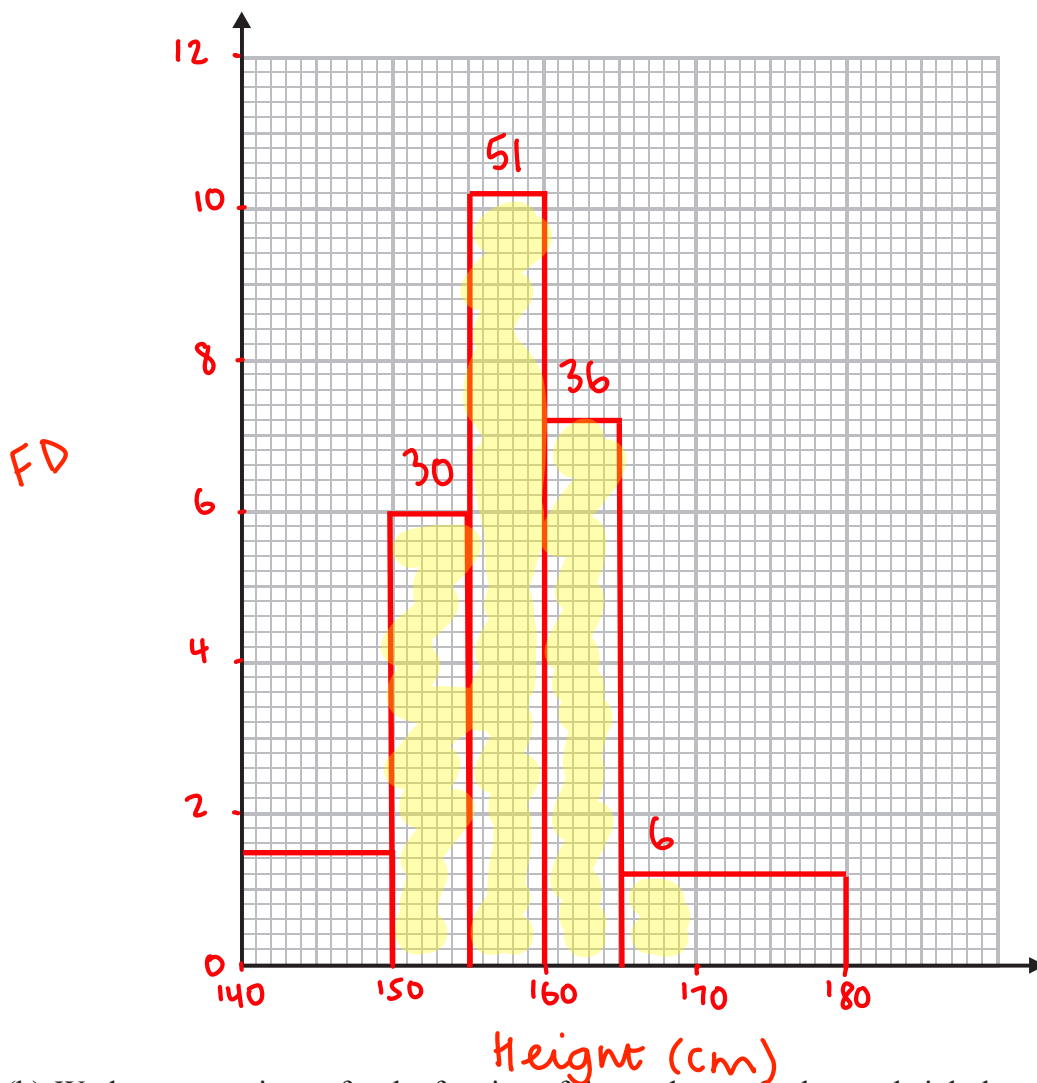
6

$$10.2$$

$$7.2$$

$$1.2$$

(a) On the grid, draw a histogram for this information.



(3)

(b) Work out an estimate for the fraction of the students who have a height between 150 cm and 170 cm.

$$30 + 51 + 36 + 6 = 123$$

$$\frac{123}{150}$$

(2)

(Total for Question 17 is 5 marks)

18 At time $t = 0$ hours a tank is full of water.

Water leaks from the tank.

At the end of every hour there is 2% less water in the tank than at the start of the hour.

The volume of water, in litres, in the tank at time t hours is V_t

Given that

$$V_0 = 2000$$

$$V_{t+1} = kV_t$$

write down the value of k .

$$k = \dots\dots\dots 0.98 \dots\dots\dots$$

(Total for Question 18 is 1 mark)



19 A triangle has vertices P , Q and R .

The coordinates of P are $(-3, -6)$

The coordinates of Q are $(1, 4)$

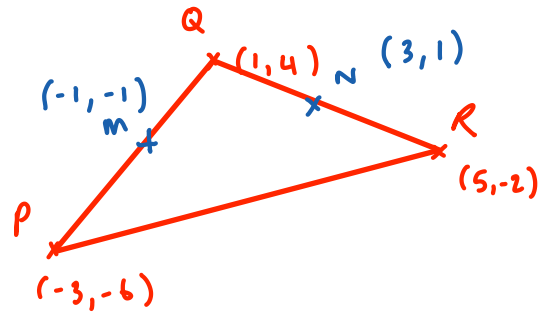
The coordinates of R are $(5, -2)$

M is the midpoint of PQ .

N is the midpoint of QR .

Prove that MN is parallel to PR .

You must show each stage of your working.



Midpoint of PQ :

$(-3, -6)$ and $(1, 4)$

$$\left(\frac{-3+1}{2}, \frac{-6+4}{2} \right) = (-1, -1)$$

Midpoint of QR :

$$\left(\frac{1+5}{2}, \frac{4+(-2)}{2} \right) = (3, 1)$$

$$\text{Gradient of } MN = \frac{1 - (-1)}{3 - (-1)} = \frac{2}{4} = \frac{1}{2}$$

$$\text{Gradient of } PR = \frac{-2 - (-6)}{5 - (-3)} = \frac{4}{8} = \frac{1}{2}$$

Same gradient $\therefore$ parallel

Tip: To find the midpoint of two coordinates, find the mean of both the x coordinates and both the y coordinates

(Total for Question 19 is 4 marks)



19 A triangle has vertices P , Q and R .

The coordinates of P are $(-3, -6)$

The coordinates of Q are $(1, 4)$

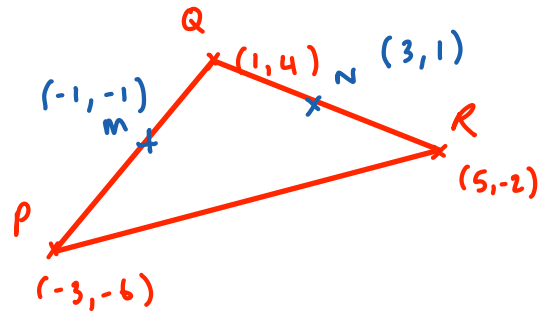
The coordinates of R are $(5, -2)$

M is the midpoint of PQ .

N is the midpoint of QR .

Prove that MN is parallel to PR .

You must show each stage of your working.



Midpoint of PQ :

$(-3, -6)$ and $(1, 4)$

$$\left(\frac{-3+1}{2}, \frac{-6+4}{2} \right) = (-1, -1)$$

Midpoint of QR :

$$\left(\frac{1+5}{2}, \frac{4+(-2)}{2} \right) = (3, 1)$$

$$\text{Gradient of } MN = \frac{1 - (-1)}{3 - (-1)} = \frac{2}{4} = \frac{1}{2}$$

$$\text{Gradient of } PR = \frac{-2 - (-6)}{5 - (-3)} = \frac{4}{8} = \frac{1}{2}$$

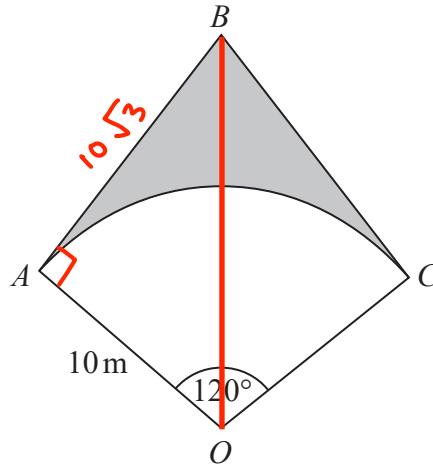
Same gradient $\therefore$ parallel

Tip: To find the midpoint of two coordinates, find the mean of both the x coordinates and both the y coordinates

(Total for Question 19 is 4 marks)



20



OAC is a sector of a circle, centre O , radius 10 m.

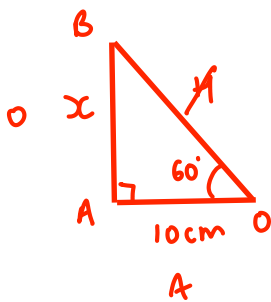
BA is the tangent to the circle at point A .

BC is the tangent to the circle at point C .

Angle $AOC = 120^\circ$

Calculate the area of the shaded region.

Give your answer correct to 3 significant figures.



S O H C A M T A

$$\tan(60) \times 10 = 10\sqrt{3}$$

$$\text{Area triangle} = \frac{10 \times 10\sqrt{3}}{2} = 86.6025..$$

$$\text{Area Sector} = \frac{120}{360} \times \pi \times 10^2 = 104.7191..$$

Shaded region =

$$(86.6025 \times 2) - 104.7191$$

$$= 68.4852..$$

68.5 m²

(Total for Question 20 is 5 marks)



22 The functions f and g are such that

$$f(x) = 5x + 3 \quad g(x) = ax + b \quad \text{where } a \text{ and } b \text{ are constants.}$$

$$g(3) = 20 \quad \text{and} \quad f^{-1}(33) = g(1)$$

Find the value of a and the value of b .

$$\begin{aligned} g(3) &= a(3) + b \\ &= 3a + b \end{aligned}$$

$$\therefore \boxed{3a + b = 20}$$

$$\begin{aligned} 5x + 3 &= 33 \\ -3 \quad -3 \\ 5x &= 30 \\ x &= 6 \end{aligned}$$

$$\begin{aligned} g(1) &= a(1) + b \\ &= a + b \end{aligned}$$

$$\therefore \boxed{a + b = 6}$$

$$\begin{array}{r} 3a + b = 20 \\ - \quad a + b = 6 \\ \hline 2a = 14 \\ a = 7 \end{array}$$

$$\begin{aligned} a + b &= 6 \\ 7 + b &= 6 \\ b &= -1 \end{aligned}$$

$$a = \underline{7}$$

$$b = \underline{-1}$$

(Total for Question 22 is 5 marks)

23 S is a geometric sequence. $\times(\sqrt{x}+1)$

- (a) Given that $(\sqrt{x}-1)$, 1 and $(\sqrt{x}+1)$ are the first three terms of S, find the value of x.
You must show all your working.

Common difference : $\times(\sqrt{x}+1)$

$$\therefore (\sqrt{x}-1)(\sqrt{x}+1) = 1$$

$$x + \sqrt{x} - \sqrt{x} - 1 = 1$$

$$x - 1 = 1$$

$$x = 2$$

$$x = 2$$

(3)

- (b) Show that the 5th term of S is $7 + 5\sqrt{2}$

$$3^{\text{rd}} : \sqrt{2} + 1$$

$$4^{\text{th}} : (\sqrt{2} + 1) \times (\sqrt{2} + 1) = 3 + 2\sqrt{2}$$

$$5^{\text{th}} : (3 + 2\sqrt{2}) \times (\sqrt{2} + 1) = 7 + 5\sqrt{2}$$

(2)

(Total for Question 23 is 5 marks)

TOTAL FOR PAPER IS 80 MARKS