

- 1 The ratio of the number of boys to the number of girls in a school is 4:5
There are 95 girls in the school.

Work out the total number of students in the school.

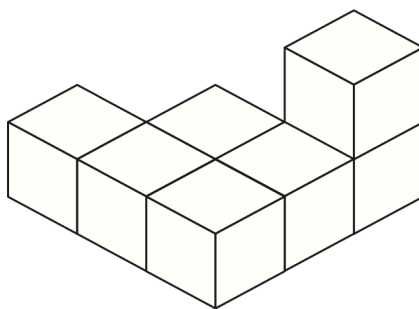
$$\begin{array}{ccc} & B : G & \\ & 4 : 5 & \\ \times 19 \swarrow & & \searrow \times 19 \\ & 76 : 95 & \end{array}$$

$$76 + 95 = 171$$

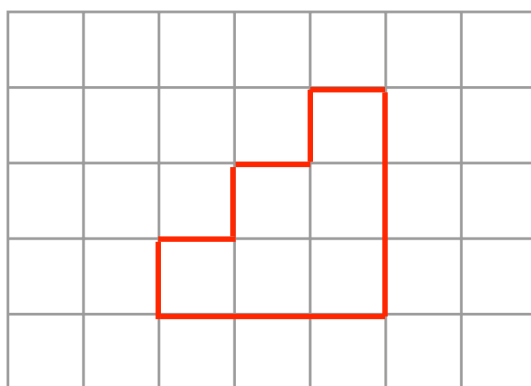
171

(Total for Question 1 is 3 marks)

- 2 The diagram represents a solid made from seven centimetre cubes.



On the centimetre grid below, draw a plan of the solid.



(Total for Question 2 is 2 marks)

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3 Make t the subject of the formula $y = \frac{t}{3} - 2a$

$$\begin{array}{rcl} & +2a & +2a \\ y+2a & = & \frac{t}{3} \\ \times 3 & & \times 3 \\ 3y+6a & = & t \end{array}$$

$$t = 3y + 6a$$

(Total for Question 3 is 2 marks)

- 4 Jim rounds a number, x , to one decimal place.
The result is 7.2

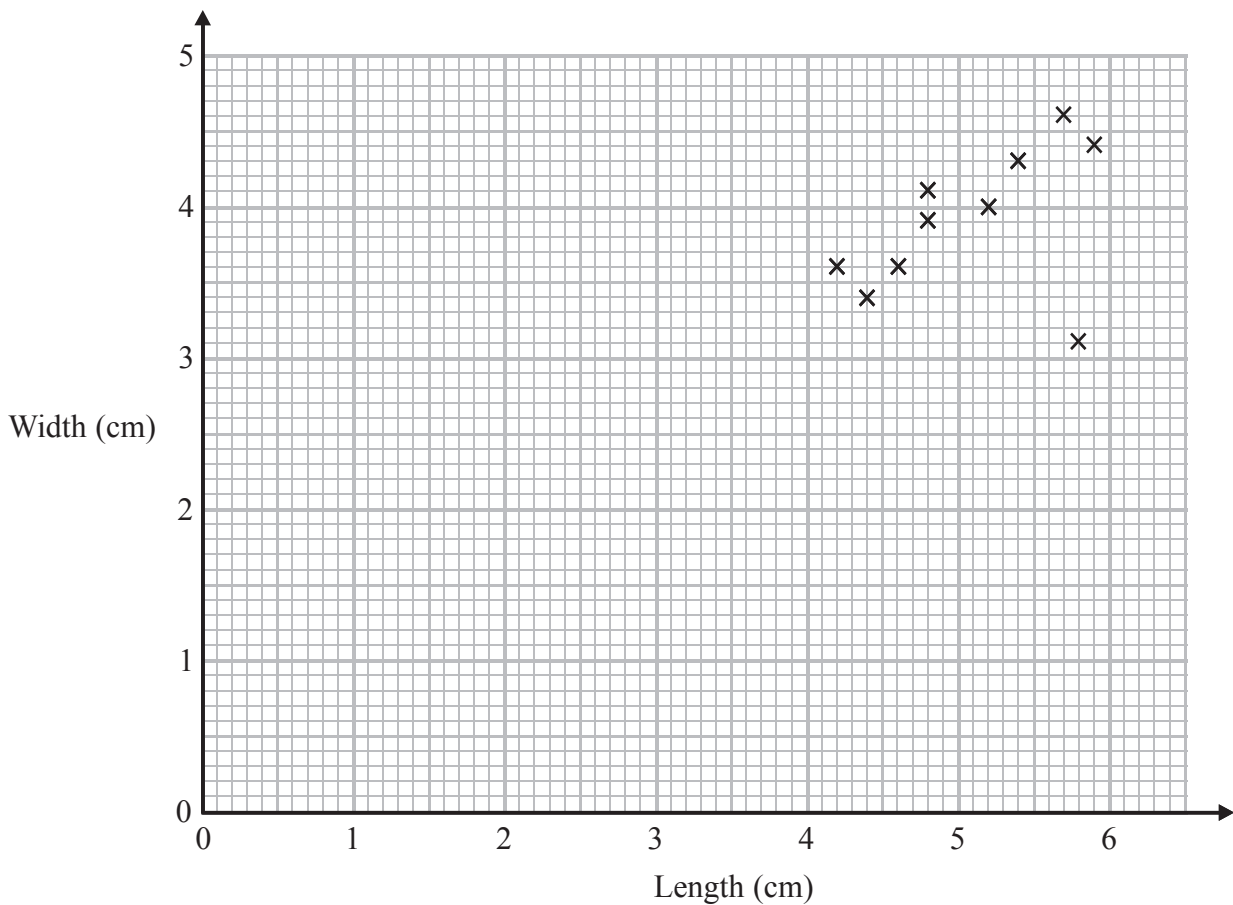
Write down the error interval for x .

$$7.15 \leq x < 7.25$$

(Total for Question 4 is 2 marks)



- 5 Katie measured the length and the width of each of 10 pine cones from the same tree. She used her results to draw this scatter graph.



- (a) Describe one improvement Katie can make to her scatter graph.

Do not have axis starting at (0,0)

(1)

The point representing the results for one of the pine cones is an outlier.

- (b) Explain how the results for this pine cone differ from the results for the other pine cones.

Very short width for its length

(1)

(Total for Question 5 is 2 marks)

- 6 At a depth of x metres, the temperature of the water in an ocean is $T^{\circ}\text{C}$.
At depths below 900 metres, T is inversely proportional to x .

T is given by

$$T = \frac{4500}{x}$$

- (a) Work out the difference in the temperature of the water at a depth of 1200 metres and the temperature of the water at a depth of 2500 metres.

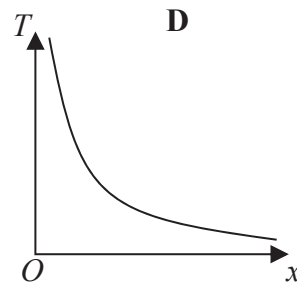
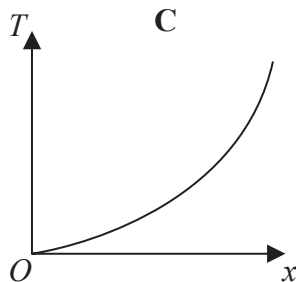
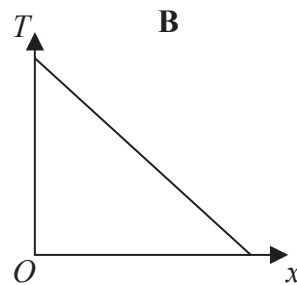
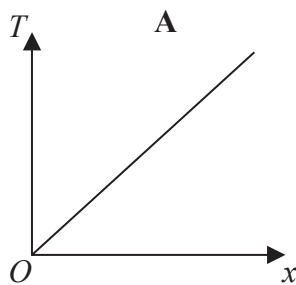
$$\frac{4500}{1200} = 3.75$$

$$\frac{4500}{2500} = 1.8$$

$$\underline{\hspace{2cm} 1.95 \hspace{2cm}}^{\circ}\text{C}$$

(3)

Here are four graphs.



One of the graphs could show that T is inversely proportional to x .

- (b) Write down the letter of this graph.

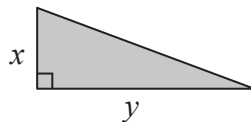
$$\underline{\hspace{2cm} D \hspace{2cm}}$$

(1)

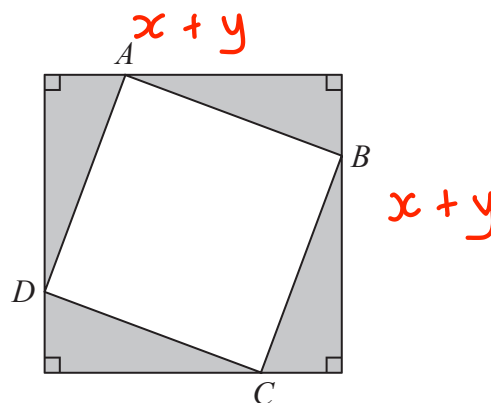
(Total for Question 6 is 4 marks)



7 Here is a right-angled triangle.



Four of these triangles are joined to enclose the square $ABCD$ as shown below.



Show that the area of the square $ABCD$ is $x^2 + y^2$

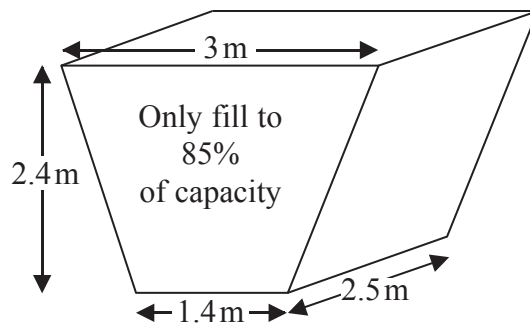
$$\begin{aligned} \text{Area Larger Square} &= (x+y)(x+y) \\ &= x^2 + xy + xy + y^2 \\ &= x^2 + 2xy + y^2 \end{aligned}$$

$$\begin{aligned} \text{Area 1 triangle} &= \frac{x \times y}{2} = \frac{xy}{2} \\ \times 4 &= \frac{4xy}{2} = 2xy \end{aligned}$$

$$\begin{aligned} \text{Area } ABCD &= x^2 + 2xy + y^2 - 2xy \\ &= x^2 + y^2 \end{aligned}$$

(Total for Question 7 is 3 marks)

- 8 The diagram shows an oil tank in the shape of a prism.
The cross section of the prism is a trapezium.



$$\frac{1}{2}(a+b)h$$

The tank is empty.

Oil flows into the tank.

After one minute there are 300 litres of oil in the tank.

Assume that oil continues to flow into the tank at this rate.

- (a) Work out how many **more** minutes it takes for the tank to be 85% full of oil.
(1 m³ = 1000 litres)

$$\text{Volume} = \frac{1}{2}(1.4 + 3) \times 2.4 \times 2.5 = 13.2 \text{ m}^3$$

$$85\% \text{ of } 13.2 = 11.22 \text{ m}^3 - 0.3 \text{ m}^3 = 10.92 \text{ m}^3 \text{ left}$$

$$1 \text{ min} = 300 \text{ L}$$

$$1 \text{ min} = 0.3 \text{ m}^3$$

$$36.4 \text{ min} = 10.92 \text{ m}^3 \quad \downarrow \times 36.4$$

36.4

minutes

(5)

The assumption about the rate of flow of the oil could be wrong.

- (b) Explain how this could affect your answer to part (a).

If the average rate was slower it would take more time

(1)

(Total for Question 8 is 6 marks)

9 Ibrar bought a house for £145 000

The value of the house depreciated by 4% in the first year.

The value of the house depreciated by 2.5% in the second year.

Ibrar says,

“ $4 + 2.5 = 6.5$ so in two years the value of my house depreciated by 6.5%”

(a) Is Ibrar right?

You must give a reason for your answer.

$$\text{No, } 0.96 \times 0.975 = 0.936$$

6.4% decrease

(2)

The value of Ibrar's house increases by $x\%$ in the third year.

At the end of the third year the value of Ibrar's house is £140 000

(b) Work out the value of x .

Give your answer correct to 3 significant figures.

$$145000 \times 0.96 \times 0.975 = 135720$$

$$\begin{array}{r|l} 135720 \times y & = 140000 \\ \div 135720 & \div 135720 \\ y & = 1.03153... \end{array}$$

3.15% increase

3.15

(3)

(Total for Question 9 is 5 marks)

10 The surface gravity of a planet can be worked out using the formula

$$g = \frac{6.67 \times 10^{-11} m}{r^2}$$

where

m kilograms is the mass of the planet

r metres is the radius of the planet

For the Earth and Jupiter here are the values of m and r .

Earth	Jupiter
$m = 5.98 \times 10^{24}$	$m = 1.90 \times 10^{27}$
$r = 6.378 \times 10^6$	$r = 7.149 \times 10^7$

Work out the ratio of the surface gravity of Earth to the surface gravity of Jupiter.

Write your answer in the form 1 : n

$$g_{\text{Earth}} = \frac{6.67 \times 10^{-11} (5.98 \times 10^{24})}{(6.378 \times 10^6)^2}$$

$$= 9.805234578$$

$$g_{\text{Jupiter}} = \frac{6.67 \times 10^{-11} (1.90 \times 10^{27})}{(7.149 \times 10^7)^2}$$

$$= 24.79641183$$

$$\begin{array}{rcl} & E : J & \\ \div 9.805 & 9.805 : 24.796 & \\ \downarrow & 1 : 2.529 & \downarrow \div 9.805 \end{array}$$

$$1 : 2.53$$

(Total for Question 10 is 3 marks)

11 Solve the simultaneous equations

$$\begin{array}{l} \times 3 \quad \times 3 \quad \times 3 \\ 2x - 4y = 19 \\ 3x + 5y = 1 \\ \times 2 \quad \times 2 \quad \times 2 \end{array}$$

$$\begin{array}{r} 6x - 12y = 57 \\ - 6x + 10y = 2 \\ \hline -22y = 55 \\ \div -22 \quad \div -22 \\ y = -2.5 \end{array}$$

$$\begin{array}{r} 3x + 5y = 1 \\ 3x + 5(-2.5) = 1 \\ 3x - 12.5 = 1 \\ +12.5 \quad +12.5 \\ 3x = 13.5 \\ \div 3 \quad \div 3 \\ x = 4.5 \end{array}$$

$x = 4.5$

$y = -2.5$

(Total for Question 11 is 4 marks)

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12 Zahra mixes 150 g of metal A and 150 g of metal B to make 300 g of an alloy

Metal A has a density of 19.3 g/cm^3 .

Metal B has a density of 8.9 g/cm^3 .

Work out the density of the alloy.

$$V = \frac{M}{D}$$



A

$$D = 19.3$$
$$M = 150 \text{ g}$$
$$V = 7.772$$

B

$$D = 8.9$$
$$M = 150 \text{ g}$$
$$V = 16.8539$$

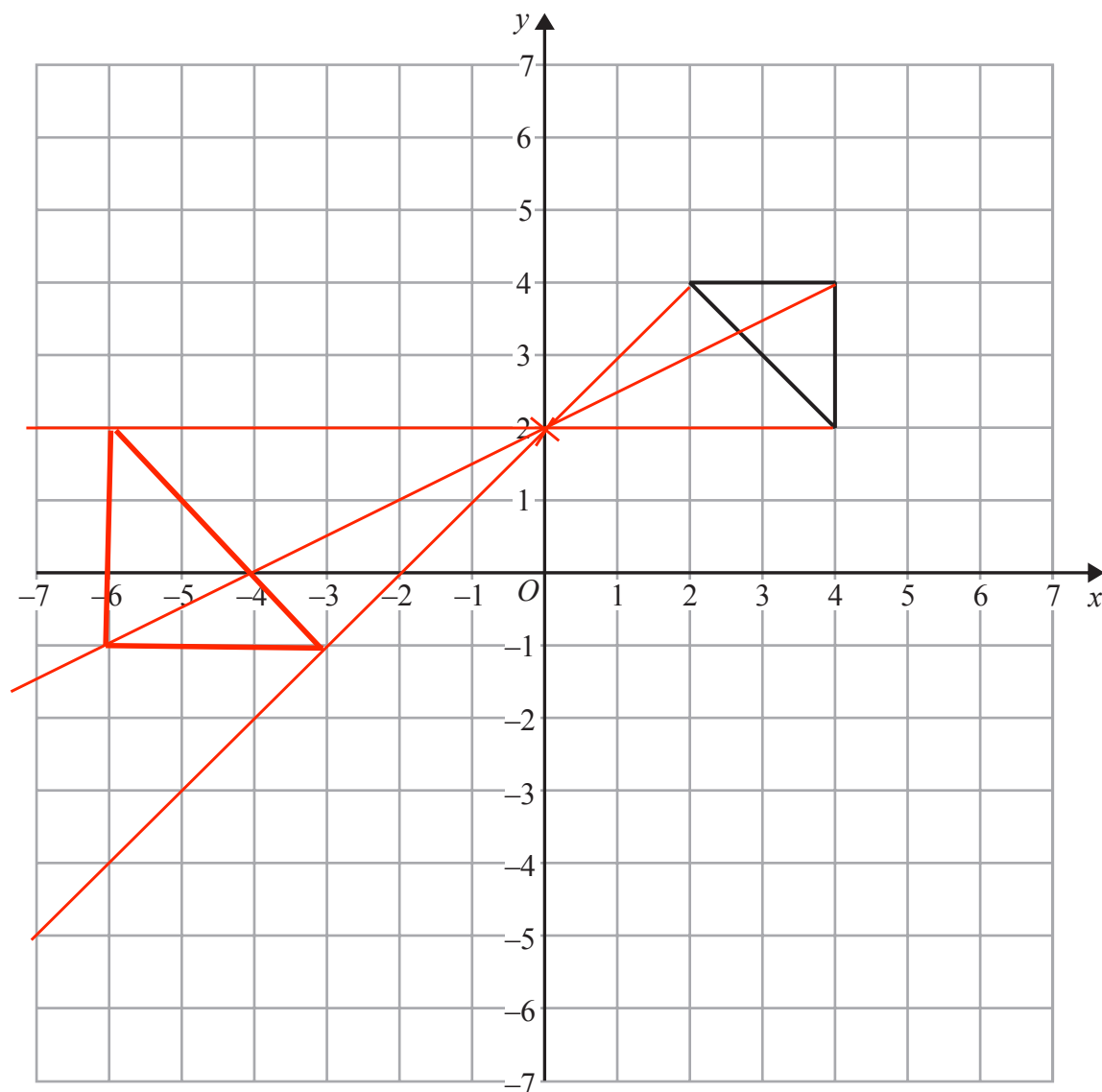
$$\text{Total Volume} = 24.626$$

$$D = \frac{M}{V} = \frac{300}{24.626} = 12.182 \dots$$

$$\underline{\underline{12.2}} \text{ g/cm}^3$$

(Total for Question 12 is 4 marks)

13



On the grid, enlarge the triangle by scale factor $-1\frac{1}{2}$, centre $(0, 2)$

(Total for Question 13 is 2 marks)



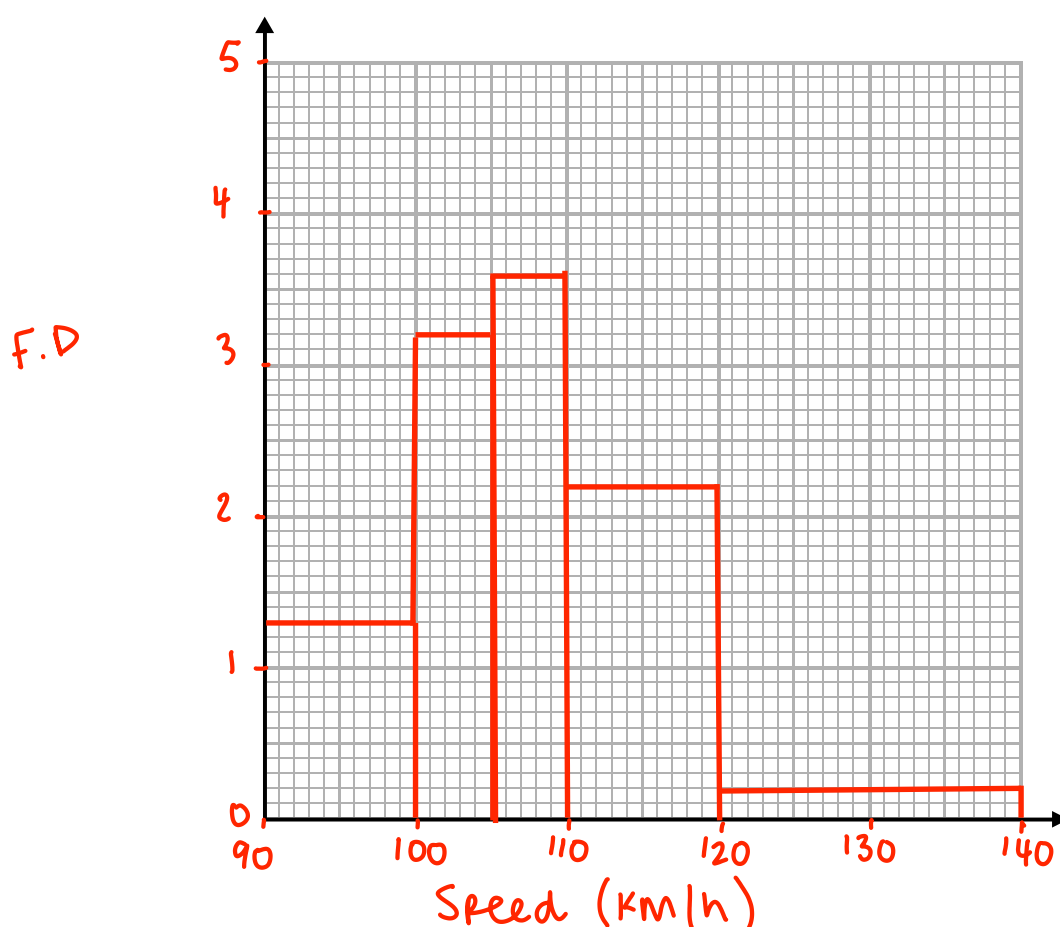
14 The table gives information about the speeds, in km/h, of 81 cars.



Speed (s km/h)	Frequency
$90 < s \leq 100$	13
$100 < s \leq 105$	16
$105 < s \leq 110$	18
$110 < s \leq 120$	22
$120 < s \leq 140$	12

FD
 $13 \div 10 = 1.3$
 3.2
 3.6
 2.2
 0.2

(a) On the grid, draw a histogram for the information in the table.



(3)

(b) Find an estimate for the median.

$$\frac{82}{2} = 41^{st}$$

$$105 + \frac{12}{18} \times 5 = 108.3$$

108.3 km/h
 (108 to 109) (2)

(Total for Question 14 is 5 marks)

15 Show that $\frac{a}{b+1} - \frac{a}{(b+1)^2}$ can be written as $\frac{ab}{(b+1)^2}$

$$\begin{aligned} & \frac{a(b+1)}{(b+1)^2} - \frac{a}{(b+1)^2} \\ &= \frac{ab+a}{(b+1)^2} - \frac{a}{(b+1)^2} = \frac{ab}{(b+1)^2} \end{aligned}$$

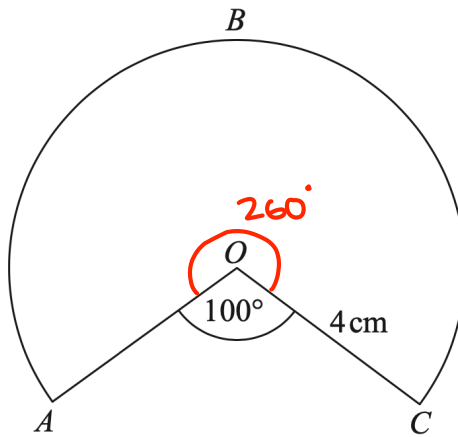
(Total for Question 15 is 2 marks)

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16 The diagram shows a sector of a circle of radius 4 cm.



Work out the length of the arc ABC .
Give your answer correct to 3 significant figures.

$$\frac{260}{360} \times \pi \times 8 = 18.1514 \dots$$

..... 18.2 cm

(Total for Question 16 is 2 marks)

- 17 The product of two consecutive positive integers is added to the larger of the two integers.

Prove that the result is always a square number.

$$n \quad \text{and} \quad n+1$$

$$n(n+1) = n^2 + n$$

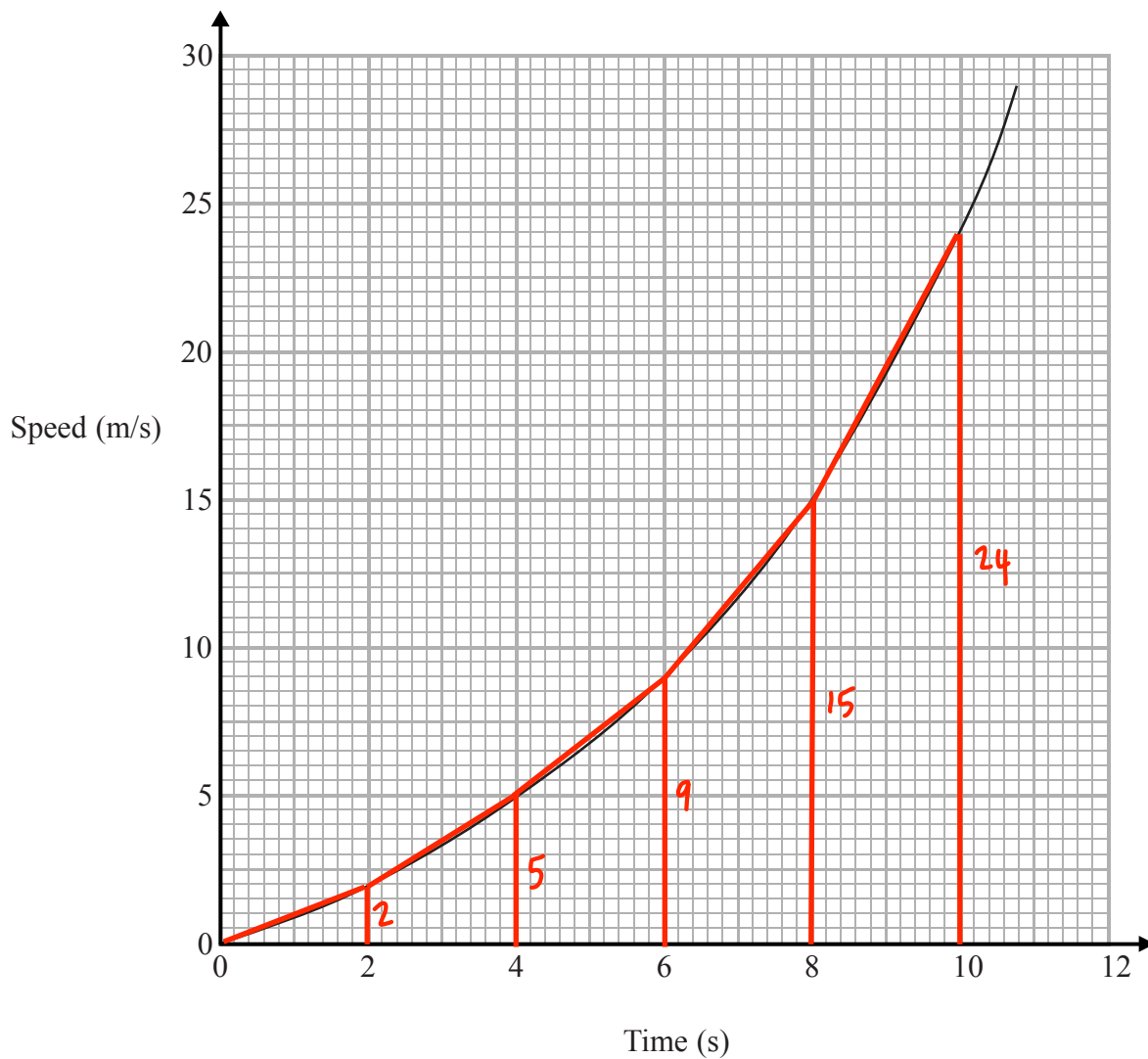
$$\begin{aligned} n^2 + n + n + 1 &= n^2 + 2n + 1 \\ &= (n+1)(n+1) \\ &= (n+1)^2 \end{aligned}$$

$\therefore$ the result is a square number for all values of n

(Total for Question 17 is 3 marks)



18 Here is a speed-time graph for a car.



- (a) Work out an estimate for the distance the car travelled in the first 10 seconds.
Use 5 strips of equal width.

$$\frac{1}{2}(2 \times 2) + \frac{1}{2}(2+5)2 + \frac{1}{2}(5+9)2$$

$$+ \frac{1}{2}(9+15)2 + \frac{1}{2}(15+24)2 = 86 \text{ m}$$

(3)

- (b) Is your answer to (a) an underestimate or an overestimate of the actual distance?
Give a reason for your answer.

Overestimate, the area between the trapeziums and the curve has been included

(1)

(Total for Question 18 is 4 marks)

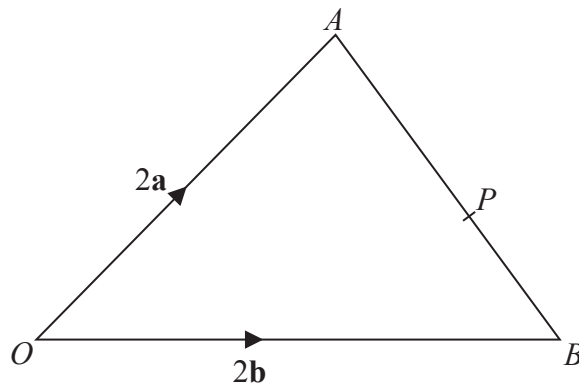
19 Prove algebraically that the recurring decimal $0.3\dot{1}\dot{8}$ can be written as $\frac{7}{22}$

$$\begin{array}{r} 100x = 31.8181818 \dots \\ - \quad x = 0.3181818 \dots \\ \hline 99x = 31.5 \\ x = \frac{31.5}{99} = \frac{315}{990} = \frac{7}{22} \end{array}$$

$\div 45$

(Total for Question 19 is 2 marks)

20



OAB is a triangle.

P is the point on AB such that $AP:PB = 5:3$

$$\vec{OA} = 2\mathbf{a}$$

$$\frac{5}{8} : \frac{3}{8}$$

$$\vec{AB} = -2\mathbf{a} + 2\mathbf{b}$$

$$\vec{OB} = 2\mathbf{b}$$

$$\vec{AP} = \frac{5}{8}(-2\mathbf{a} + 2\mathbf{b}) = -\frac{5}{4}\mathbf{a} + \frac{5}{4}\mathbf{b}$$

$$\vec{OP} = k(3\mathbf{a} + 5\mathbf{b}) \text{ where } k \text{ is a scalar quantity.}$$

Find the value of k .

$$\begin{aligned} \vec{OP} &= \vec{OA} + \vec{AP} = 2\mathbf{a} - \frac{5}{4}\mathbf{a} + \frac{5}{4}\mathbf{b} \\ &= \frac{3}{4}\mathbf{a} + \frac{5}{4}\mathbf{b} \\ &= \frac{1}{4}(3\mathbf{a} + 5\mathbf{b}) \end{aligned}$$

$$\frac{1}{4}$$

(Total for Question 20 is 4 marks)

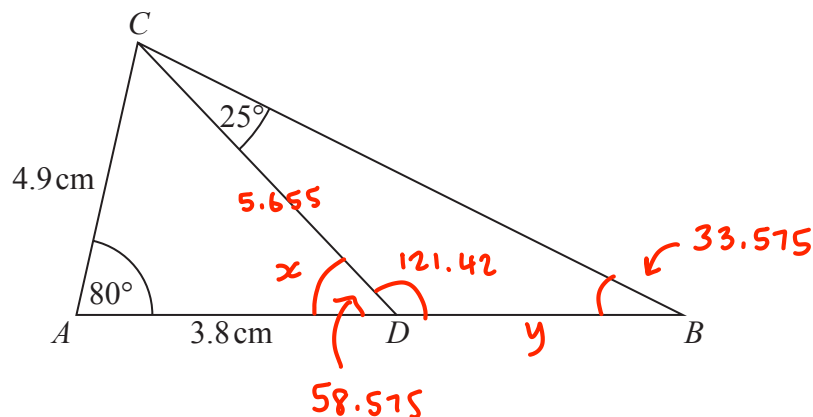
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21



ABC is a triangle.
 D is a point on AB .

Work out the area of triangle BCD .
 Give your answer correct to 3 significant figures.

$$\begin{aligned}
 CD &= a^2 = b^2 + c^2 - 2bc \cos A \\
 a^2 &= (4.9)^2 + (3.8)^2 - 2(4.9)(3.8) \times \cos(80) \\
 a^2 &= 31.98.. \\
 \sqrt{\quad} \quad \sqrt{\quad} \\
 a &= 5.655
 \end{aligned}$$

$$\angle ADC = \frac{\sin x}{4.9} = \frac{\sin(80)}{5.655}$$

$$\sin x = \frac{\sin(80)}{5.655} \times 4.9 = 0.8533..$$

$$x = \sin^{-1}(0.8533..) = 58.515$$

$$DB = \frac{y}{\sin(25)} = \frac{5.655}{\sin(33.515)}$$

$$y = \frac{5.655}{\sin(33.515)} \times \sin(25) = 4.32$$

$$\begin{aligned}
 \frac{1}{2} ab \sin C &= \frac{1}{2} (5.655)(4.32) \times \sin(121.42) \\
 &= 10.421..
 \end{aligned}$$

10.4 cm²

(Total for Question 21 is 5 marks)



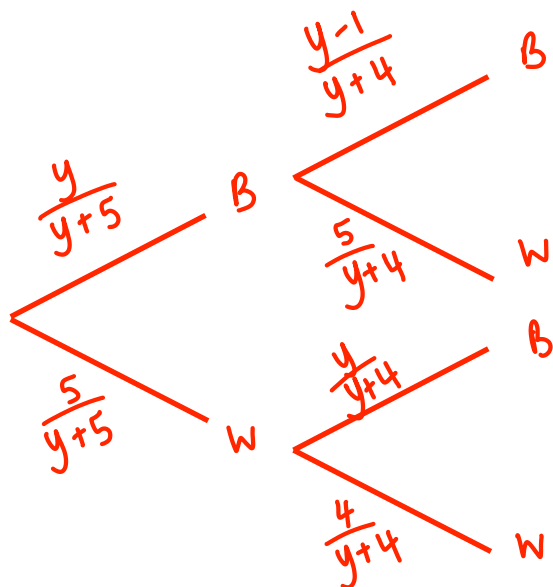
22 There are y black socks and 5 white socks in a drawer.

$$\text{Total: } y + 5$$

Joshua takes at random two socks from the drawer.

The probability that Joshua takes one white sock and one black sock is $\frac{6}{11}$

(a) Show that $3y^2 - 28y + 60 = 0$



$$W, B = \frac{5}{y+5} \times \frac{y}{y+4} = \frac{5y}{y^2+9y+20}$$

$$B, W = \frac{y}{y+5} \times \frac{5}{y+4} = \frac{5y}{y^2+9y+20}$$

$$\frac{5y}{y^2+9y+20} + \frac{5y}{y^2+9y+20} = \frac{6}{11}$$

$$\frac{10y}{y^2+9y+20} = \frac{6}{11} \quad \text{Tip: Cross multiply to solve}$$

$$110y = 6y^2 + 54y + 120$$

$$-110y$$

$$-110y$$

$$0 = 6y^2 - 56y + 120$$

$$\div 2 \quad 0 = 3y^2 - 28y + 60$$

(4)

(b) Find the probability that Joshua takes two black socks.

$$3y^2 - 28y + 60 = 0$$

$$a = 3, b = -28, c = 60$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$\frac{-(-28) \pm \sqrt{(-28)^2 - 4(3)(60)}}{2(3)}$$

$$y = 6 \quad \text{and} \quad y = 10/3$$

Tip: y has to be a whole number because we are talking about socks

$$P(B, B) = \frac{6}{11} \times \frac{5}{10} = \frac{30}{110}$$

$$\frac{30}{110}$$

(3)

(Total for Question 22 is 7 marks)

23 (a) Write $2x^2 + 16x + 35$ in the form $a(x + b)^2 + c$ where a , b , and c are integers.

$$= 2(x^2 + 8x + 17.5)$$

$$= 2[(x + 4)^2 + 1.5]$$

$$= 2(x + 4)^2 + 3$$

$$2(x + 4)^2 + 3$$

(3)

(b) Hence, or otherwise, write down the coordinates of the turning point of the graph of $y = 2x^2 + 16x + 35$

$$(-4, 3)$$

(1)

(Total for Question 23 is 4 marks)

TOTAL FOR PAPER IS 80 MARKS