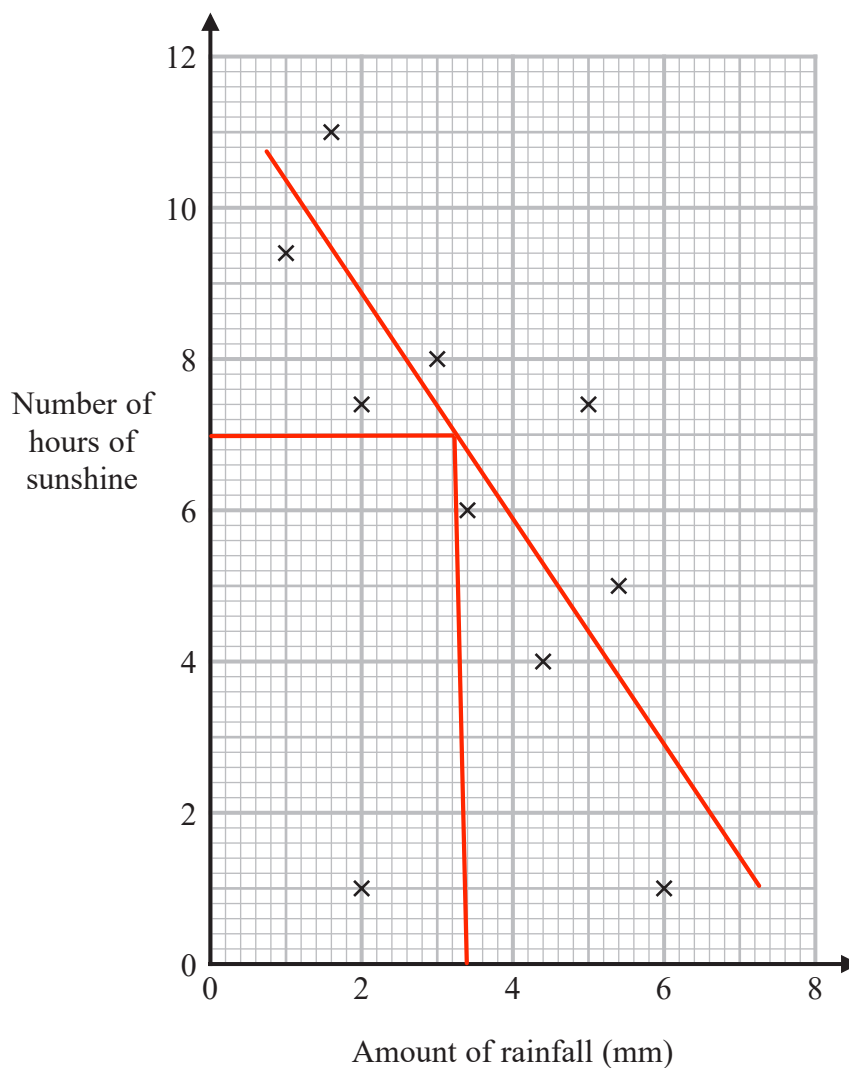


- 1 The scatter graph shows information about the amount of rainfall, in mm, and the number of hours of sunshine for each of ten English towns on the same day.



One of the points is an outlier.

- (a) Write down the coordinates of this point.

(2 , 1)
(1)

- (b) Ignoring the outlier, describe the relationship between the amount of rainfall and the number of hours of sunshine.

As the amount on rainfall decreases, the amount of sunshine increases

(1)

On the same day in another English town there were 7 hours of sunshine.

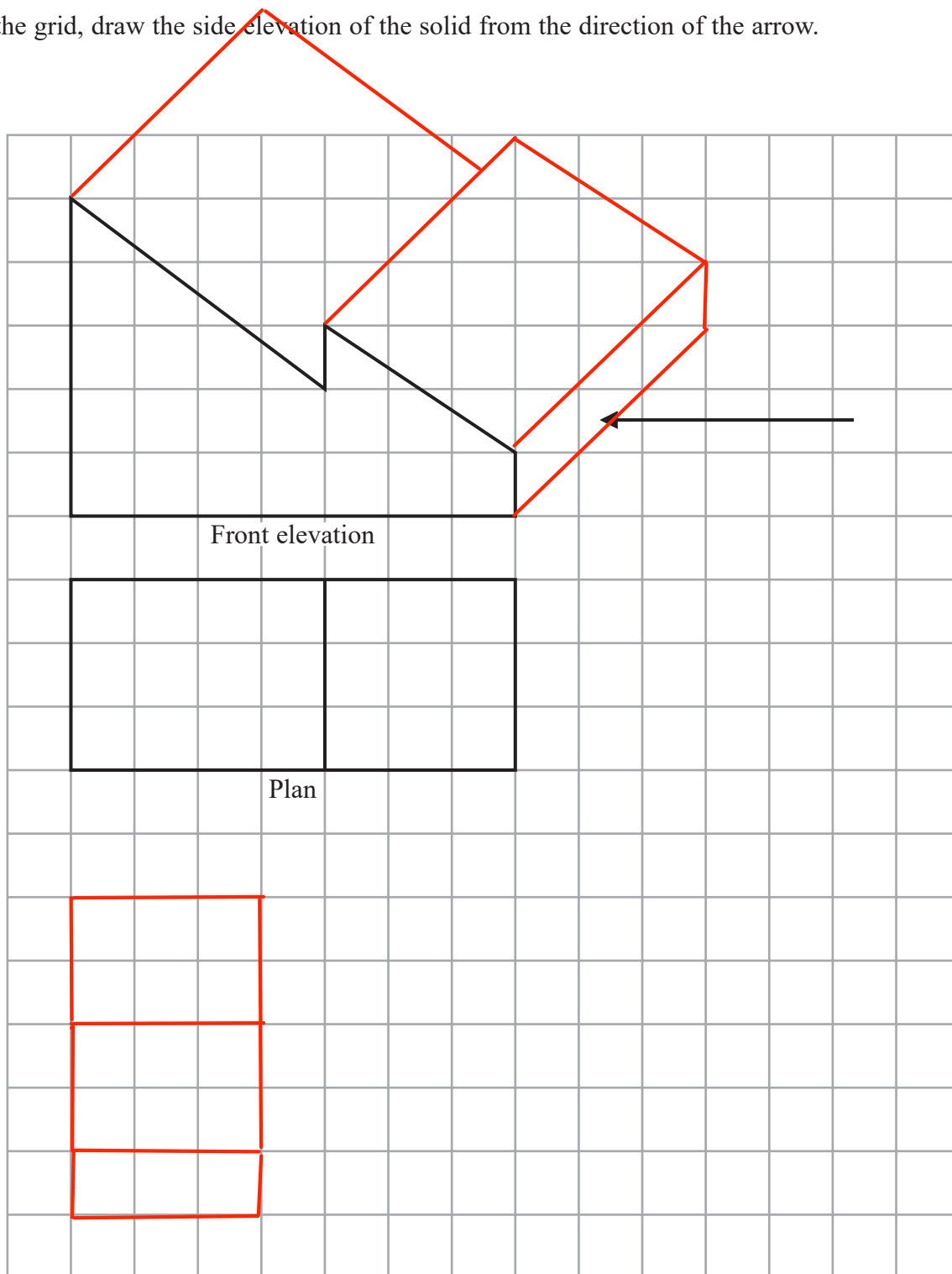
- (c) Using the scatter graph, estimate the amount of rainfall in this town on this day.

3.4 mm
(3 to 4) (2)

(Total for Question 1 is 4 marks)

- 2 The front elevation and the plan of a solid are shown on the grid.

On the grid, draw the side elevation of the solid from the direction of the arrow.



(Total for Question 2 is 2 marks)



- 3 Here are the first five terms of an arithmetic sequence.

1 7 13 19 25 31

- (a) Find an expression, in terms of n , for the n th term of this sequence.

$$6n + 1$$

(2)

The n th term of a different sequence is $8 - 6n$

- (b) Is -58 a term of this sequence?

You must show how you get your answer.

$$\begin{array}{rcl}
 8 - 6n & = & -58 \\
 + 6n & & + 6n \\
 \hline
 8 & = & 6n - 58 \\
 + 58 & & + 58 \\
 \hline
 66 & = & 6n \\
 \div 6 & & \div 6 \\
 \hline
 11 & = & n
 \end{array}$$

yes

(2)

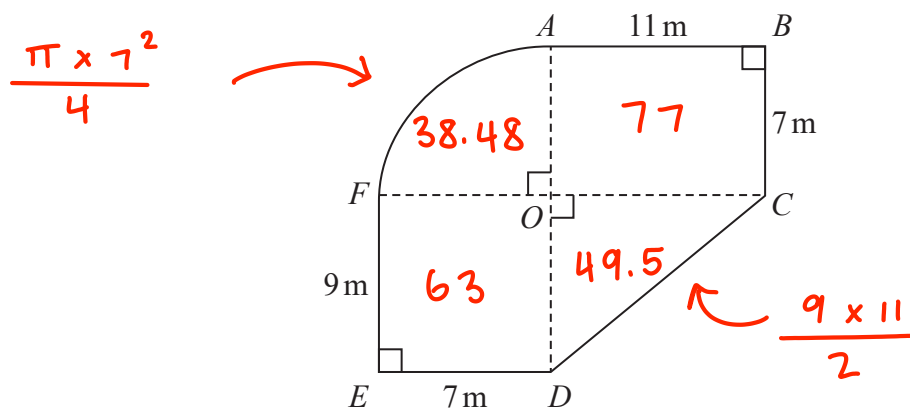
(Total for Question 3 is 4 marks)

- 4 The diagram shows a plan of Jason's garden.

$ABCO$ and $DEFO$ are rectangles.

CDO is a right-angled triangle.

AFO is a sector of a circle with centre O and angle $AOF = 90^\circ$



Jason is going to cover his garden with grass seed.

Each bag of grass seed covers 14 m^2 of garden.

Each bag of grass seed costs £10.95

Work out how much it will cost Jason to buy all the bags of grass seed he needs.

$$\begin{aligned} \text{Total area} &= 38.48 + 77 + 63 + 49.5 \\ &= 227.98 \end{aligned}$$

$$227.98 \div 14 = 16.28 \quad (17 \text{ bags})$$

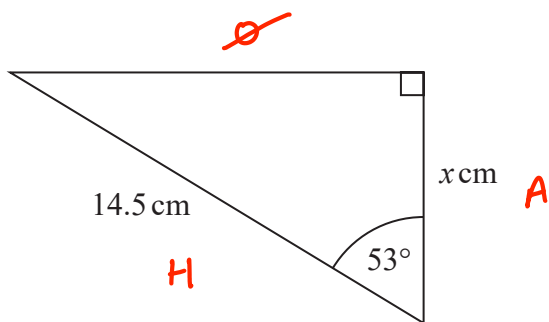
$$17 \times 10.95 = £186.15$$

£ 186.15

(Total for Question 4 is 5 marks)



5



S^O H C^A H T^O A

H

Work out the value of x .

Give your answer correct to 3 significant figures.



$$\cos(53) \times 14.5$$

$$x = 8.73$$

(Total for Question 5 is 2 marks)

- 6 Ella invests £7000 for 2 years in an account paying compound interest.

In the first year, the rate of interest is 3%

In the second year, the rate of interest is 1.5%

Work out the value of Ella's investment at the end of 2 years.

$$7000 \times 1.03 = 7210$$

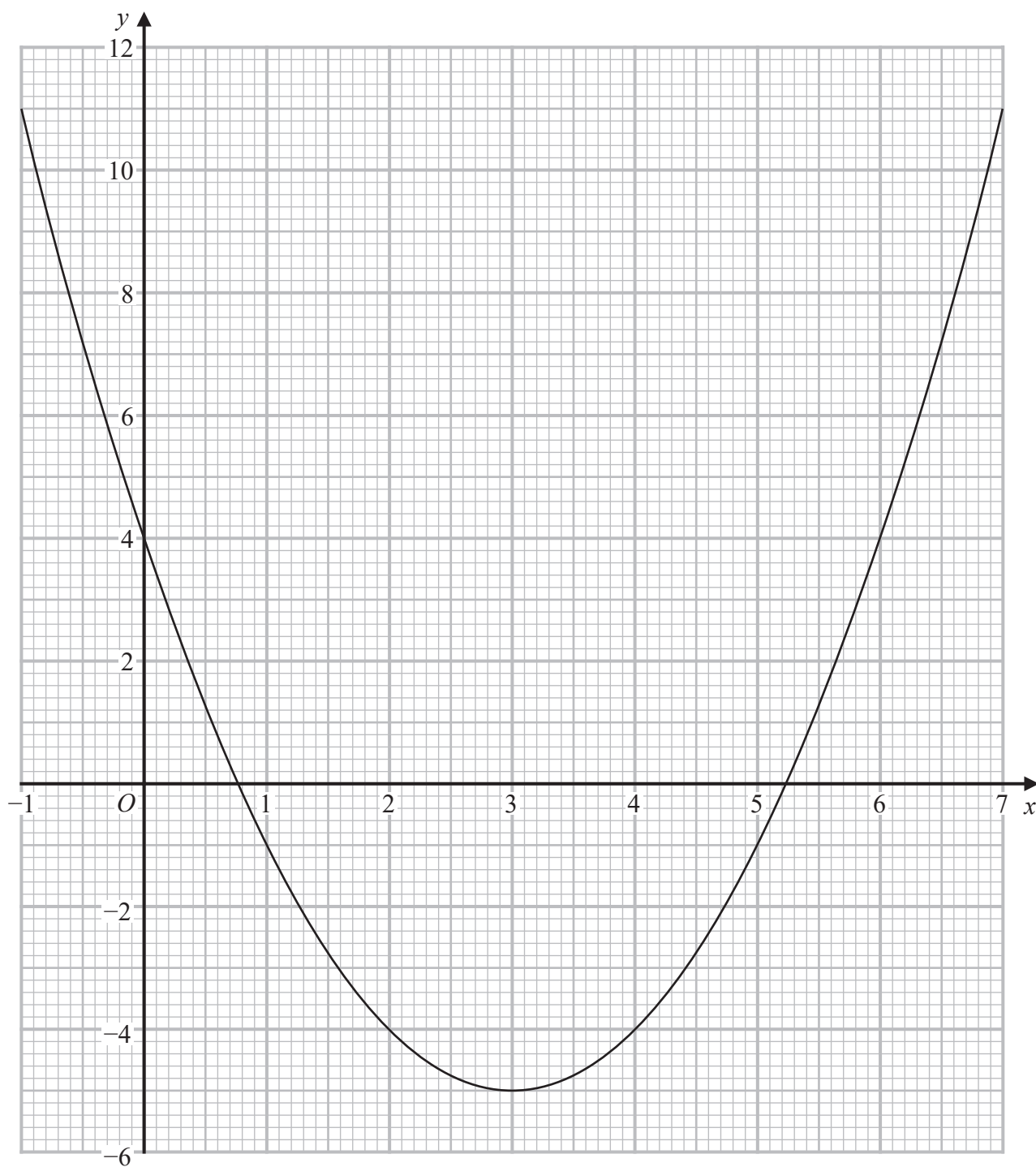
$$7210 \times 1.015 = 7318.15$$

£ 7318.15

(Total for Question 6 is 3 marks)



7 Here is the graph of $y = x^2 - 6x + 4$



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- (a) Write down the y intercept of the graph of $y = x^2 - 6x + 4$

4

(1)

- (b) Write down the coordinates of the turning point of the graph of $y = x^2 - 6x + 4$

(3 , -5)
(1)

- (c) Use the graph to find estimates for the roots of $x^2 - 6x + 4 = 0$

0.75, 5.25

(2)
(0.7 to 0.9 / 5.1 to 5.3)

(Total for Question 7 is 4 marks)

- 8 Chanda buys a necklace for £120
She sells the necklace for £135

Work out her percentage profit.

$$\frac{\text{Change}}{\text{Original}} \times 100$$

$$\frac{15}{120} \times 100$$

$$12.5\%$$

(Total for Question 8 is 3 marks)

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9 Here are the equations of two straight lines.

$$y = \frac{1}{2}x - 6$$

Oscar says that these lines are parallel.

Is Oscar correct?

You must give a reason for your answer.

$$\begin{array}{l} 6y = 3x + 7 \\ \div 6 \quad \div 6 \\ y = \frac{3}{6}x + \frac{7}{6} \end{array}$$

$$\frac{3}{6} = \frac{1}{2}$$

Yes, both have a gradient of $\frac{1}{2}$

(Total for Question 9 is 2 marks)

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10 Aaliyah bought a car.

In the first year after she bought the car, its value depreciated at a rate of 23% per annum.

In the second year after she bought the car, its value depreciated at a rate of 19% per annum.

At the end of the second year the car was worth £10914.75

What was the value of the car when Aaliyah bought it?

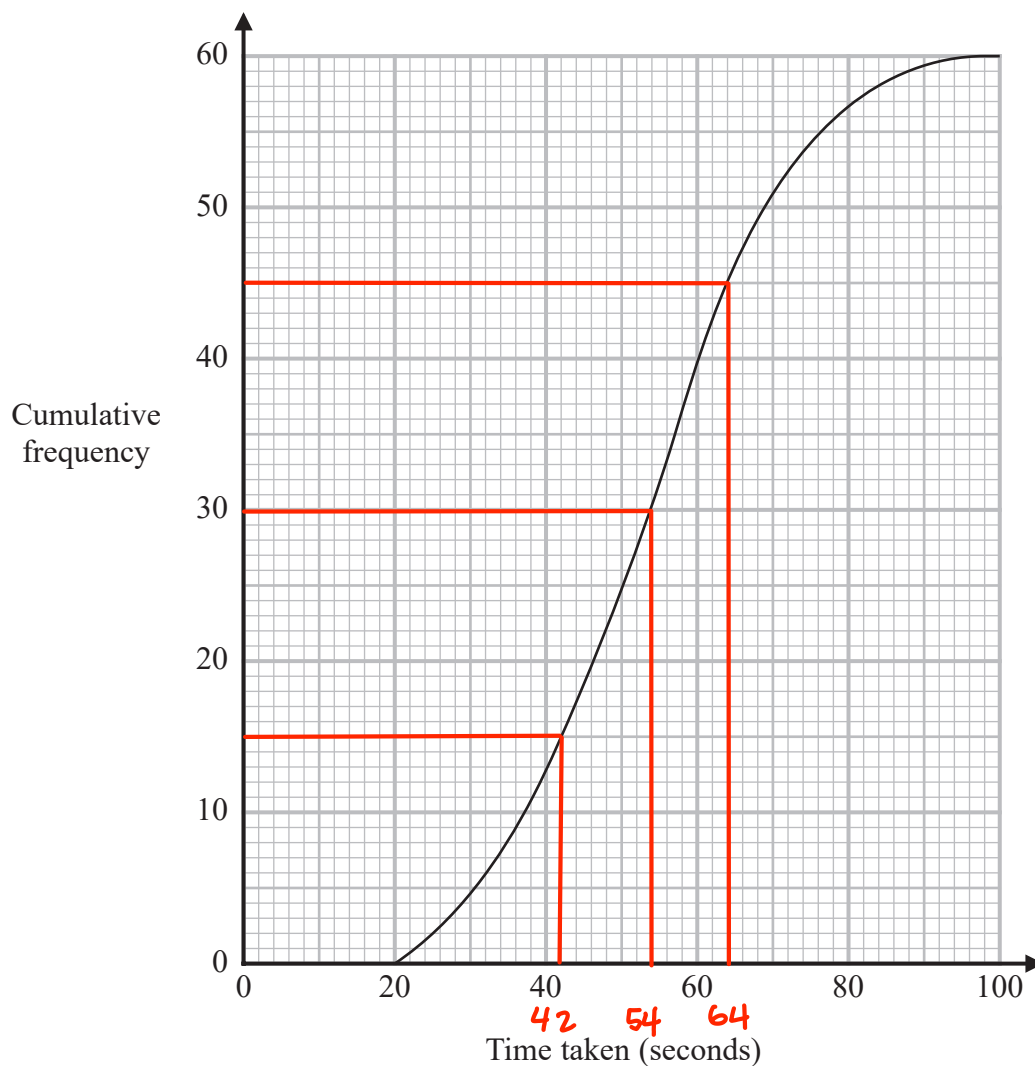
$$\begin{array}{rcl}
 x \times 0.77 \times 0.81 & = & 10914.75 \\
 \div 0.81 & & \div 0.81 \\
 x \times 0.77 & = & 13415 \\
 \div 0.77 & & \div 0.77 \\
 x & = & 17500
 \end{array}$$

£ 17500

(Total for Question 10 is 3 marks)

11 In an experiment, 60 students each completed a puzzle.

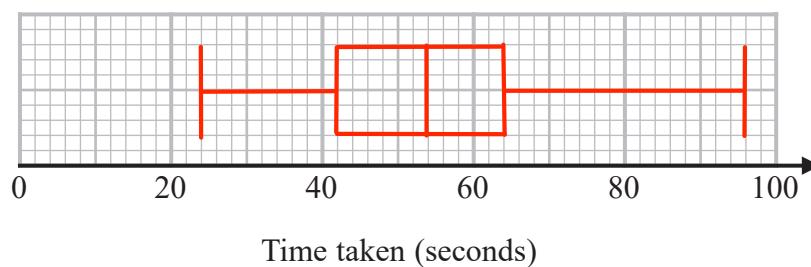
The cumulative frequency graph shows information about the times taken for the 60 students to complete the puzzle.



For these 60 students,

the least time taken was 24 seconds
the greatest time taken was 96 seconds.

On the grid below, draw a box plot for the distribution of the times taken by the students.



(Total for Question 11 is 3 marks)



12 The number of insects in a population at the start of the year n is P_n

The number of insects in the population at the start of year $(n + 1)$ is P_{n+1} where

$$P_{n+1} = kP_n$$

Given that k has a constant value of 1.13

$$= 1.3 \times P_n$$

- (a) find out how many years it takes for the number of insects in the population to double.
You must show how you get your answer.

$$(1.13)^n > 2$$

$$1.13^5 = 1.84 \dots$$

$$1.13^6 = 2.08 \dots$$

6

(2)

The value of k actually increases year on year from its value of 1.13 in year 1

- (b) How does this affect your answer to part (a)?

it will take less years

(1)

(Total for Question 12 is 3 marks)

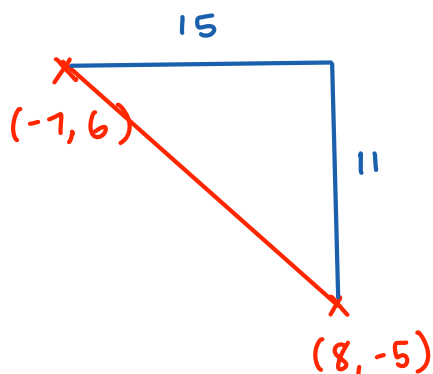
13 A and B are points on a centimetre grid.

A is the point with coordinates $(-7, 6)$

B is the point with coordinates $(8, -5)$

Work out the length of AB .

Give your answer correct to 1 decimal place.



$$a^2 + b^2 = c^2$$

$$15^2 + 11^2 = 346$$

$$\sqrt{346} = 18.6$$

18.6

..... cm

(Total for Question 13 is 2 marks)

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14 Using algebra, prove that $1.0\dot{6}\dot{2}$ can be written as $1\frac{14}{225}$

Tip: There is 1 recurring digit so we multiply by 10

$$\begin{array}{r} 10x = 0.\overset{5}{\cancel{1}}\overset{1}{2}\cancel{2}\cancel{2}\dots \\ - \quad x = 0.0\cancel{6}\cancel{2}\cancel{2}\dots \\ \hline \end{array}$$

$$\begin{array}{l} 9x = 0.56 \\ \div 9 \quad \div 9 \\ x = \frac{0.56}{9} = \frac{56}{900} \end{array} \xrightarrow{\div 4} \frac{14}{225}$$

$$\text{so } 1.0\dot{6}\dot{2} = 1\frac{14}{225}$$

(Total for Question 14 is 3 marks)

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- 15 Faiza is studying the population of rabbits in a park.
She wants to estimate the number of rabbits in the park.

On Monday she catches a random sample of 20 rabbits in the park, marks each rabbit with a tag and releases them back into the park.

On Tuesday she catches a random sample of 42 rabbits in the park.
12 of the rabbits are marked with a tag.

- (a) Find an estimate for the number of rabbits in the park.

$$\frac{20}{x} = \frac{12}{42}$$

$\xrightarrow{\times 1.6}$
 $\xleftarrow{\times 1.6}$

$$42 \times 1.6 = 70$$

70

(3)

Albie is studying the population of rabbits in a wood.

One day, he catches 55 rabbits and finds that 40 of these rabbits are marked with a tag.

Albie estimates there are 50 rabbits in the wood.

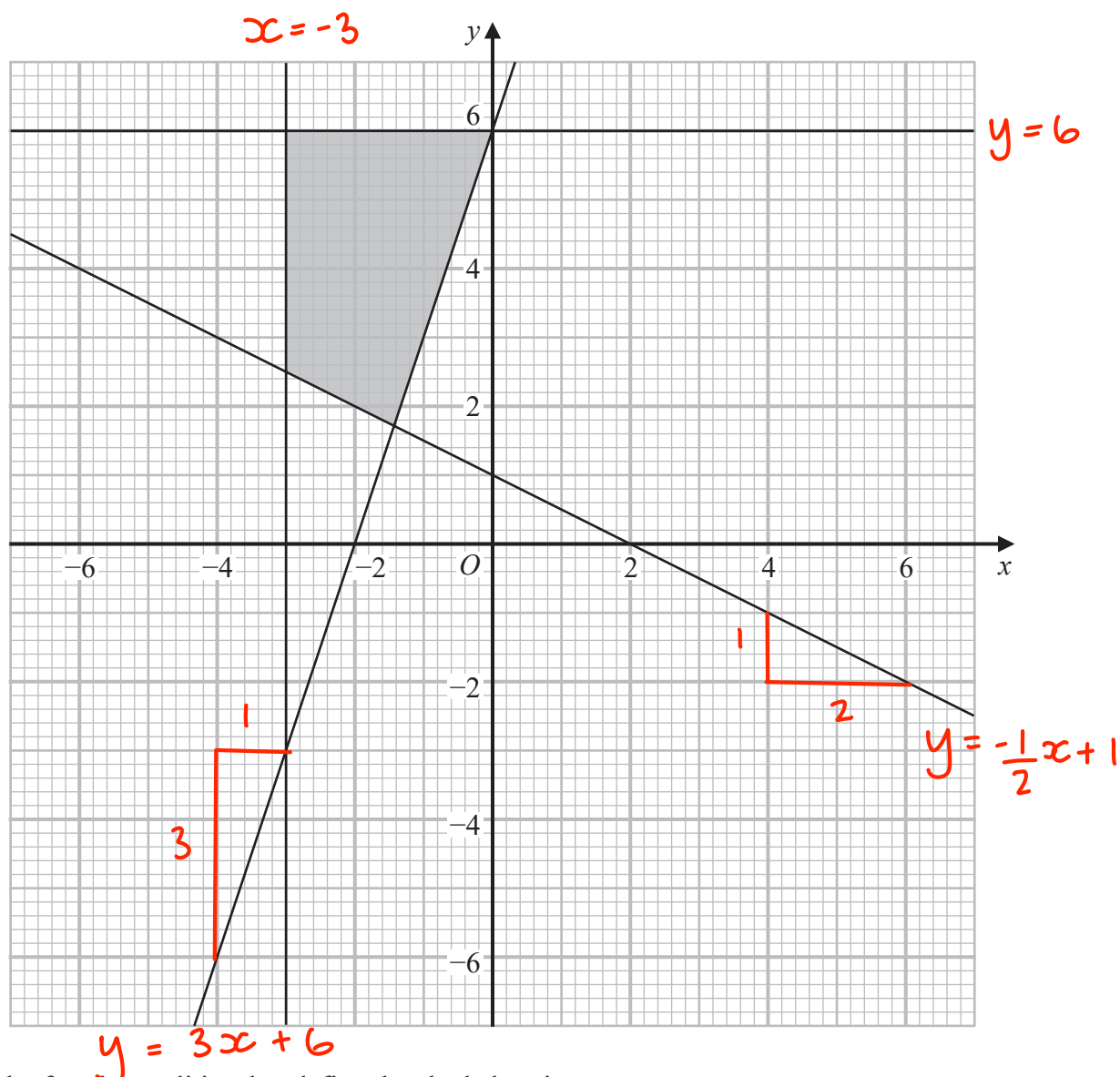
- (b) Explain why Albie's estimate cannot be correct.

If he caught 55, there must be at least 55 rabbits

(1)

(Total for Question 15 is 4 marks)

16 The shaded region shown on the grid is bounded by four straight lines.



Find the four inequalities that define the shaded region.

$$x \geq -3$$

$$y \leq 6$$

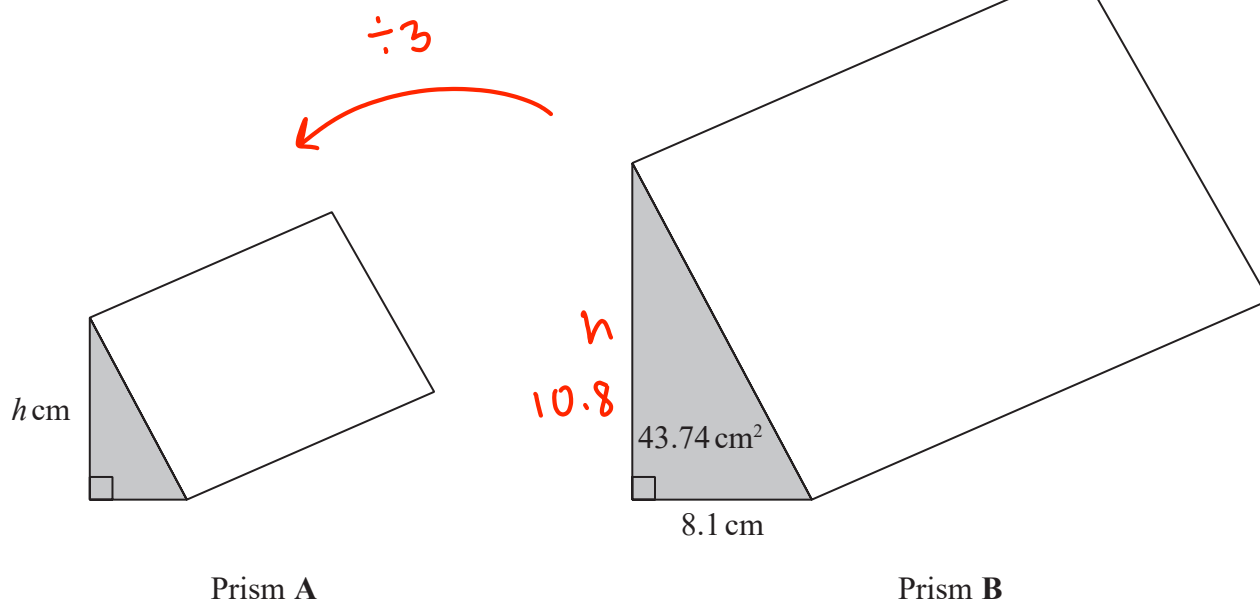
$$y \geq -\frac{1}{2}x + 1$$

$$y \geq 3x + 6$$

(Total for Question 16 is 4 marks)



17 The diagram shows two similar solid triangular prisms, **A** and **B**.



The volume of prism **A** is 58.806 cm^3

The volume of prism **B** is 1587.762 cm^3

The cross section of each prism is a right-angled triangle.

For prism **B**

the length of the base of the triangle is 8.1 cm

the area of the triangle is 43.74 cm^2

The height of the triangle for prism **A** is $h \text{ cm}$.

Work out the value of h .

$$\text{Volume SF} = 27$$

$$\text{Length SF} = \sqrt[3]{27} = 3$$

$$\begin{array}{rcl} \frac{1}{2} \times 8.1 \times h & = & 43.74 \\ \times 2 & & \times 2 \\ 8.1 \times h & = & 87.48 \\ \div 8.1 & & \div 8.1 \\ h & = & 10.8 \end{array}$$

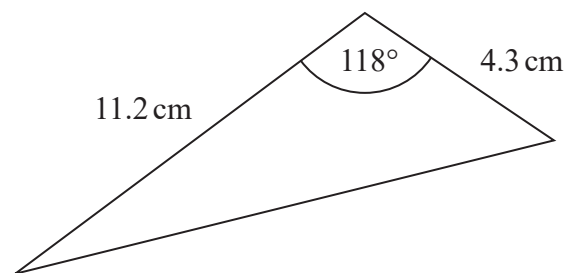
$$10.8 \div 3 = 3.6$$

$$h = 3.6$$

(Total for Question 17 is 4 marks)



18 Here is a triangle.



Work out the area of the triangle.

Give your answer correct to 3 significant figures.

$$\begin{aligned}
 & \frac{1}{2} ab \sin C \\
 &= \frac{1}{2} \times 11.2 \times 4.3 \times \sin(118) \\
 &= 21.26\dots
 \end{aligned}$$

21.3 cm²

(Total for Question 18 is 2 marks)

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19 Solve $6x^2 + 5x - 6 = 0$

$$\frac{- (5) \pm \sqrt{(5)^2 - 4(6)(-6)}}{2(6)}$$

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$a = 6, b = 5, c = -6$$

$$x = 0.6 \text{ OR } -1.5$$

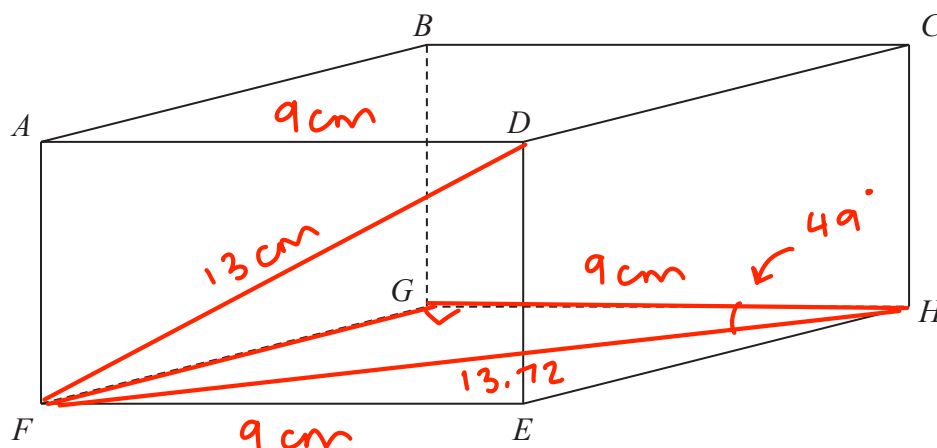
(Total for Question 19 is 3 marks)

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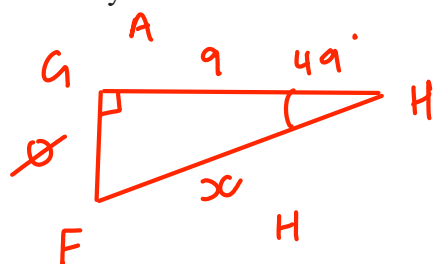
20 $ABCDEFGH$ is a cuboid.



$AD = 9 \text{ cm}$
 $FD = 13 \text{ cm}$
 Angle $GHF = 49^\circ$

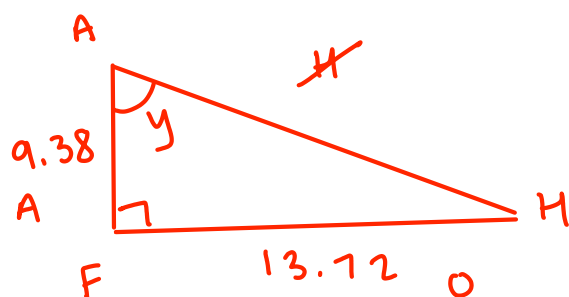
$S^{\circ} H C^A H T^{\circ} A$

Work out the size of angle FAH .
 Give your answer correct to the nearest degree.



$$\frac{9}{\cos(49)} = 13.72$$

$$AF = \sqrt{13^2 - 9^2} = 9.38$$



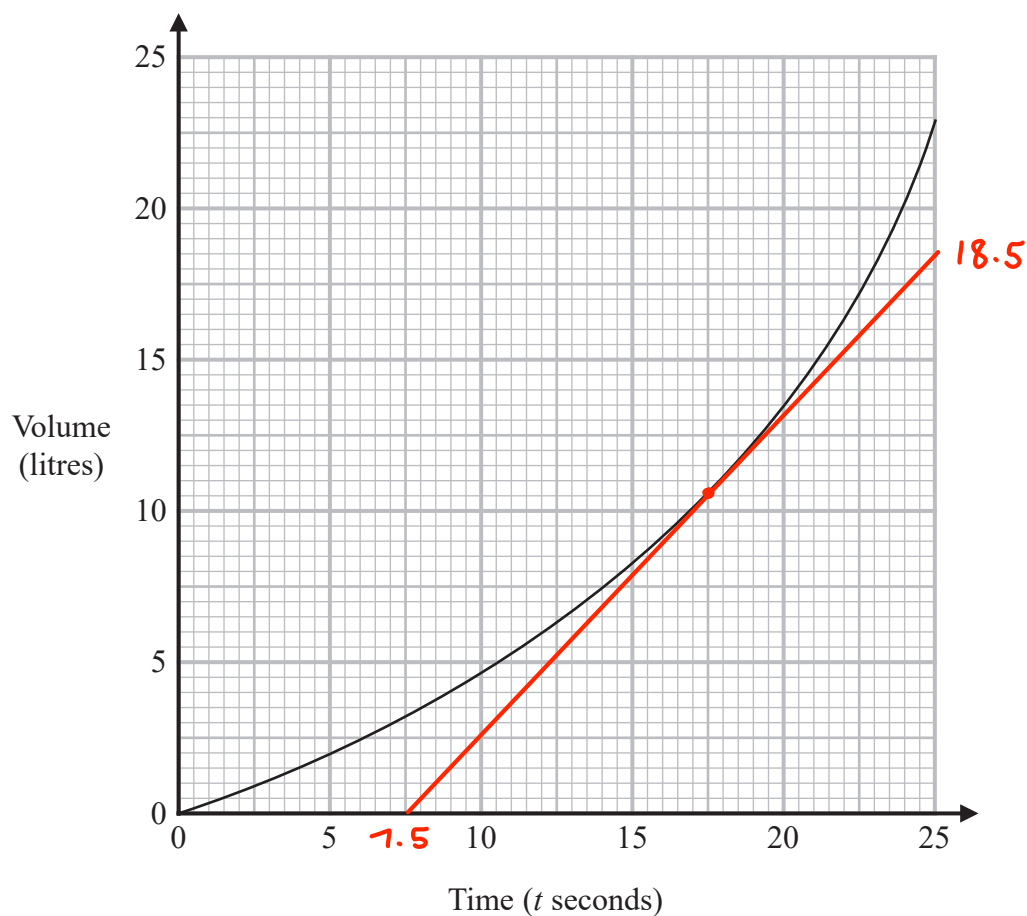
$T^{\circ} A$

$$\tan^{-1}\left(\frac{13.72}{9.38}\right) = 55.63..$$

56

(Total for Question 20 is 4 marks)

- 21 The graph below gives the volume, in litres, of water in a container t seconds after the water starts to fill the container.



- (a) Calculate an estimate for the gradient of the graph when $t = 17.5$
You must show how you get your answer.

$$\frac{\text{rise}}{\text{run}} = \frac{18.5}{17.5} = 1.06$$

$$\frac{1.06}{(0.9 \text{ to } 1.2)}^{(3)}$$

- (b) Describe fully what the gradient in part (a) represents.

The increase in volume (litres) per second

(1)

(Total for Question 21 is 4 marks)



22 $f(x) = \sqrt[3]{x}$
 $g(x) = 2x + 3$

$h(x) = fg(x)$

Find $h^{-1}(x)$

$$fg(x) = \sqrt[3]{2x + 3} = h(x)$$

$h^{-1}(x) :$

$$\begin{array}{lcl} y & = & \sqrt[3]{2x + 3} \\ y^3 & = & 2x + 3 \\ -3 & & -3 \\ \hline y^3 - 3 & = & 2x \\ \div 2 & & \div 2 \\ \hline \frac{y^3 - 3}{2} & = & x \end{array}$$

$$h^{-1}(x) = \frac{x^3 - 3}{2}$$

(Total for Question 22 is 3 marks)

10.55 10.65

- 23 A race is measured to have a distance of 10.6 km, correct to the nearest 0.1 km. (1 dp)
 Sam runs the race in a time of 31 minutes 48 seconds, correct to the nearest second.
 1908 seconds $\rightarrow$ 1907.5 1908.5
 Sam's average speed in this race is V km/hour.

By considering bounds, calculate the value of V to a suitable degree of accuracy.
 You must show all your working and give a reason for your answer.

$$S = \frac{D}{T}$$

$$S_L = \frac{D_L}{T_u} = \frac{10.55}{0^{\circ}0^{\circ}1908.5^{\circ}} = 19.900..$$

$$S_u = \frac{D_u}{T_L} = \frac{10.65}{0^{\circ}0^{\circ}1907.5^{\circ}} = 20.099..$$

Tip: Use the time button on your calculator to convert seconds into hours

$$V = 20 \text{ km/h}$$

Both upper and lower bound round to 20 to the nearest whole number

(Total for Question 23 is 5 marks)

24 A circle has equation $x^2 + y^2 = 12.25$

$$\sqrt{12.25} = 3.5$$

The point P lies on the circle.

The coordinates of P are $(2.1, 2.8)$

The line L is the tangent to the circle at point P .

Find an equation of L .

Give your answer in the form $ax + by = c$, where a , b and c are integers.

Gradient OP

$$= \frac{2.8 - 0}{2.1 - 0} = \frac{4}{3}$$

$$\text{Gradient } L = -\frac{3}{4}$$

$$y = -\frac{3}{4}x + c$$

$$2.8 = -\frac{3}{4}(2.1) + c$$

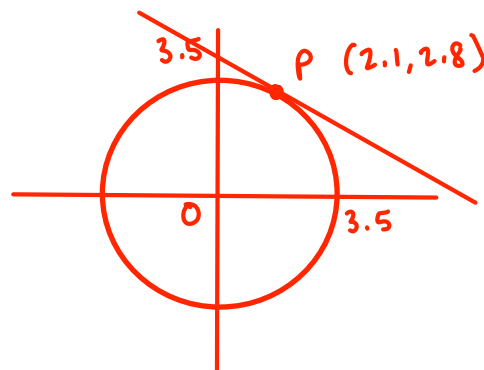
$$2.8 \quad | = \quad -\frac{63}{40} + c$$

$$+\frac{63}{40} \quad | \quad +\frac{63}{40}$$

$$\frac{35}{8} \quad | = \quad c$$

$$y = -\frac{3}{4}x + \frac{35}{8} \quad \times 8$$

$$8y = -6x + 35$$



$$6x + 8y = 35$$

(Total for Question 24 is 4 marks)

TOTAL FOR PAPER IS 80 MARKS